

# Aircraft Design Project 

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## 1-Abstract \& Theoretical Discussion

First thing to do after getting an offer for an aircraft, is to gather around some peer aircraft (an aircraft which is close to the wanted aircraft in the mission based on its Category, Size, Weights, Range and etc.) data and try to design based on their data,it is obvious that,as much as your peer aircrafts are more, your work would be better.

Then we need to choose a target aircraft (an aircraft which parameters are very close to our mission specification). then we'are ready to start designing.

The first step in designing an aircraft, is to estimate the weight of the aircraft during take-off. To weigh the take-off weight we first need to obtain a range of these weights according to data base then initial Take-off weight gain will be estimated. Our values need to be obtained for $W_{\text {OE tent }}$ and $W_{E \text { tent }}$ and for this purpose we need to calculate the Mff. Then with considering the amount of $W_{E}$ and $W_{T . O}$ form data base we can gain the values of $W_{T . O}, W_{E}$ for mission aircraft, earned percentage of error must be below 0.5 percent, while the take-off weight of the aircraft is calculated.

At the end,we need to chart some graphs. these graphs are named 'sizing' and they are 8 ,first we introduce them:

1. Stall Speed
2. Take-off Field Length
3. Landing Field Length
4. Climb Rate
5. Cruise Speed
6. Ceiling
7. Time to Climb
8. Maneuvering

The purpose of calculating these spoken Sizing's is to chart T/W vs W/S (Matching Diagram) and specify the design area.this design area is a part of above graphs which in it,designing is much more economic.
Sizing information about each of the following calculations method will be explained in detail. Finally, by drawing Matching Diagram and specify the design area, the point at which the maximum W/S and the lowest T/W is such that the lowest weight and cost will be reached.

In the next step we will show you our mission.

## 2-Mission Specifications

| Mission Specifications for a Transport Jet |  |
| :---: | :---: |
| Payload | 400 Passengers at 175 lbs and 60 lbs of Baggage Each. |
| Crew | 2 Pilots and 8 Flight Attendants at 175 lbs and 30 lbs of Baggage Each. |
| Range | $6,500 \mathrm{~nm}$, followed by 0.75 hour loiter, followed by a 300 nm flight to alternate. |
| Altitude | 35,000 ft (for the design range). |
| Climb | Direct climb to 35,000 ft in 20 minutes. At max. WTO is desired. |
| Cruise Speed | $\mathrm{M}=0.84$ at $35,000 \mathrm{ft}$ |
| Take-off and Landing | FAR 25 take-off field length $10,500 \mathrm{ft}$ and 8000 ft landing field length at $100^{\circ} \mathrm{F}$ (Hot day) in Kerman Airport. |
| Power Plants | Two Turbofans |
| Pressurization | $6,000 \mathrm{ft}$. cabin at $35,000 \mathrm{ft}$. |
| Certification Base | FAR 25 |



As we said before, we have to find a target aircraft.

## 3-Introducing the Target Airplane

According to the mission, from the data base collected, the closest aircraft in flight range, speed cruise and weights, is Boeing 777-300ER.

Boeing 777-300ER, first flew on 24 February 2003 and on 10 May 2004 aviation fleet was entered. With two pilots and capable of carrying 365 passengers in a three classes fly. The price of this model is between 250 to 279 million dollars.

In undercarriage discussion it has retractable tricycle with two main wheels and a retractable guide wheels on the nose.

327565 lbs fuel capacity and also has two engines (General Electric turbofans (GE90-115B)).
The aircraft is capable of flying at a distance of 7705 nm or 14,270 kilometers.
Compared to the 777-300 model has a stronger engine and the ability to carry more fuel in the wings.

Everything is set now and we need to start working!

## 4-First Step

Take a little glimpse at what we are about to do:
First using the mission we obtain $W_{\text {Crew }} \& W_{P L}$.

$$
\begin{aligned}
& \mathrm{W}_{\mathrm{PL}}=400 \times(175+60)=94000 \mathrm{lbs} \\
& \mathrm{~W}_{\text {Crew }}=10 \times(175+30)=2050 \mathrm{lbs}
\end{aligned}
$$

Then we need to come up with a guess for $W_{T . O}$ (using peer aircrafts data.).
After that with weight ratios in any phase of flight we are going to calculate Mff.
And, using Mff amount to calculate $W_{O E_{\text {tent }}} \& W_{E_{\text {tent }}}$.
Now with the use of peer aircrafts data we draw $\log W_{T . O}$ vs $\log W_{E}$ in Excel linear regression plot and erasing data which are far above the regression line obtained. The values A and B are now determined.

$$
\log W_{T . O}=A+B \log W_{E}
$$

They should be close to book values Roskam said, then using $W_{E}$ we obtain the maximum allowed take-off weight.

Now, the difference between $W_{E_{\text {tent }}}$ and $W_{E}$ is obtained. By using computer software's and try error method (with changing the amount of $W_{T . O}$ we have guessed before.) we should make the difference come to zero. Having the final step repeat then we have a suitable amount of $W_{T . O}$.

Now we are going to use the above method:

### 4.1.1-Estimating Take-Off Weight

First, we need an initial guess for estimating take-off weight of the aircraft according to peer aircrafts data. $W_{P L}$, cruise speed and range of the peer aircrafts are specified.

| Airplane model | $W_{P L}$ | $R$ | $V_{\text {CRUISE }}$ | $W_{T .0}$ |
| :---: | :---: | :---: | :---: | :---: |
| B777-200LR | 69740 | 11000 | 0.84 | 766000 |
| B777-200ER | 131000 | 7730 | 0.84 | 656000 |
| B777-300 | 147200 | 5950 | 0.84 | 660000 |
| B777-300ER | 87120 | 9470 | 0.84 | 775000 |
| A350-1000 | 46050 | 8000 | 0.85 | 681000 |
| B777-F | 226000 | 9300 | 0.84 | 766800 |
| B747-400M | 137521 | 7214 | 0.84 | 875000 |
| B747- <br> 400DOMESTIC | 246000 | 1805 | 0.85 | 833000 |

Given the range defined in the mission and the payload weight, and from peer aircrafts data we can estimate the take-off weight.so we guessed:

$$
W_{\text {T.O }}^{\text {Guess }} ⿵=680000 \mathrm{lbs}
$$

### 4.1.2-Calculating Mission Fuel Fraction

$$
M_{f f}=\frac{w_{9}}{w_{8}} \times \frac{w_{8}}{w_{7}} \times \frac{w_{7}}{w_{6}} \times \frac{w_{6}}{w_{5}} \times \frac{w_{5}}{w_{4}} \times \frac{w_{4}}{w_{3}} \times \frac{w_{3}}{w_{2}} \times \frac{w_{2}}{w_{1}} \times \frac{w_{1}}{w_{T . O}}
$$

Some weight fraction given in Table 2.1 Roskam:
$\frac{W_{1}}{W_{T . O}}$
$\frac{W_{2}}{W_{1}}$
$\frac{W_{3}}{W_{2}}$
$\frac{W_{4}}{W_{3}}$
$\frac{W_{7}}{W_{6}}$
$\frac{W_{9}}{W_{8}}$
0.990
0.990
0.995
0.980
0.990
0.992

As a result, only weight ratio in phases, Cruise, Loiter and Fly to alternate needs to be calculated.

### 4.1.3-Calculating Cruise to Climb Weight

To calculate the weight ratio in the cruise phase, we use the following formula:

$$
\mathrm{R}_{\mathrm{Cr}}=\left(\frac{\mathrm{V}}{\mathrm{C}_{\mathrm{j}}}\right)_{\mathrm{Cr}} \times\left(\frac{\mathrm{L}}{\mathrm{D}}\right)_{\mathrm{Cr}} \times \ln \left(\frac{\mathrm{W}_{4}}{\mathrm{~W}_{5}}\right)
$$

R is the range of aircraft, Cj represents the amount of fuel consumption at this point, and V shows the speed of cruise in Mach term that is defined in the mission, and V should be based on Knots.

To calculate the speed of Cruise in Knots:

$$
\mathrm{V}_{\mathrm{Cr}}=\frac{\mathrm{M} \sqrt{32.2 \gamma \mathrm{RT}}}{1.6878}=482.27 \text { Knots }
$$

And we have:

$$
\begin{aligned}
& \gamma=1.4 \\
& \mathrm{R}=53.3 \mathrm{ft} * \mathrm{lbf} / \mathrm{lbm} \\
& \mathrm{~T}=389.958 \mathrm{R}
\end{aligned}
$$

And also we have to correct the height change, that's why we divided the velocity to 1.6878.
In order to find the range of cruise, we have:

$$
\mathrm{R}_{\mathrm{Cr}}=\mathrm{R}-\mathrm{R}_{\mathrm{Climb}}
$$

To calculate the range of climb we need the speed of climb.

$$
\mathrm{R}_{\text {Climb }}=\frac{20}{60} \times \mathrm{V}_{\text {Climb }}
$$

Climb speed mode is given by the formula:

$$
\mathrm{V}_{\mathrm{Climb}}=\frac{\mathrm{V}_{\mathrm{Cr}}+\mathrm{V}_{\mathrm{T} . \mathrm{O}}}{2}
$$

$\mathrm{V}_{\mathrm{T} . \mathrm{O}}$ for target aircraft (B777-300ER) is 186.83 Knots.
Then:

$$
\mathrm{V}_{\mathrm{Climb}}=\frac{186.83+482.27}{2}=334.55 \mathrm{Kts}
$$

Now we have the speed of climb:

$$
\mathrm{R}_{\mathrm{Climb}}=111.52 \mathrm{~nm}
$$

Now with climb range we can calculate cruise range.

$$
\mathrm{R}_{\mathrm{Cr}}=6388.49 \mathrm{~nm}
$$

In Table 2.2 Roskam range of (L/D) Cruise for transport jet aircraft is given, then with using it (L/D) cruise mode can be guessed and using the following formula to check it and correct it.

$$
\left.\frac{\mathrm{L}}{\mathrm{D}}\right)_{\mathrm{MAX}}=0.5 \sqrt{\frac{\pi \mathrm{AR}}{\mathrm{KC} \mathrm{C}_{\mathrm{Df}}}}
$$

Some known parameters:

$$
\begin{gathered}
\mathrm{K}=1.2 \\
\mathrm{C}_{\mathrm{Df}}=0.0165 \\
\mathrm{AR}=9.813606827
\end{gathered}
$$

And some to calculate:

$$
\begin{aligned}
\left.\frac{\mathrm{L}}{\mathrm{D}}\right)_{\mathrm{MAX}}= & \left.\frac{\mathrm{L}}{\mathrm{D}}\right)_{\text {Loiter }}=0.5 \times \sqrt{\frac{\pi \times 9.813606827}{1.2 \times 0.0165}} \\
& \left.\left.\frac{\mathrm{~L}}{\mathrm{D}}\right)_{\text {Cruise }}=0.866 \frac{\mathrm{~L}}{\mathrm{D}}\right)_{\text {Loiter }} \\
& \left.\left.\frac{\mathrm{L}}{\mathrm{D}}\right)_{\text {Fly to alternate }}=0.6 \frac{\mathrm{~L}}{\mathrm{D}}\right)_{\mathrm{MAX}}
\end{aligned}
$$

So:

$$
\begin{gathered}
\left.\frac{\mathrm{L}}{\mathrm{D}}\right)_{\text {Cruise }}=17.08 \\
\left.\frac{\mathrm{~L}}{\mathrm{D}}\right)_{\mathrm{MAX}}=19.73 \\
\left.\frac{\mathrm{~L}}{\mathrm{D}}\right)_{\text {Fly to alternate }}=11.835
\end{gathered}
$$

According to calculations made and Mission, the amount of cruise weight fraction obtained using Breguet equations.

$$
\frac{W_{5}}{W_{4}}=0.7
$$

### 4.1.4-Calculating Loiter to Cruise Weight

Using this formula to calculate loiter endurance:

$$
\left.E_{\text {Loiter }}=\frac{1}{C_{j_{\text {Loiter }}}} \times \frac{L}{D}\right)_{\text {Loiter }} \times \ln \left(\frac{W_{5}}{W_{6}}\right)
$$

According to the mission, endurance in this phase is 0.75 hour. In Roskam table, ${ }^{*} \mathrm{Cj}$ loiter must not exceed one unit of Cj During the cruise phase. Therefore, we consider 0.6 for Cj in loiter phase.
According to the information given in the definition of Mission, the amount of loiter to cruise weight is:

$$
\frac{W_{6}}{W_{5}}=0.977
$$

### 4.1.5-Calculating Flying to Alternate Over Loiter Weight

To calculate the weight ratio of the phase Fly to alternate the following formula is used:

$$
R_{F l y}=\left(\frac{V}{C_{j}}\right)_{F l y} \times\left(\frac{L}{D}\right)_{F l y} \times \ln \left(\frac{W_{7}}{W_{8}}\right)
$$

According to the mission, range in this phase is equal to 300 nm and V and Cj are 250 Knots (according FAR25) and 0.9 , respectively.
$\mathrm{L} / \mathrm{D}$ in this phase is equal to 11.835 :

$$
\left(\frac{L}{D}\right)_{F l y}=0.6\left(\frac{L}{D}\right)_{\text {Loiter }}
$$

So then:

$$
\frac{W_{8}}{W_{7}}=0.913
$$

### 4.1.6-Finalizing Mff

Due to the weight ratios calculated, now Mff can be calculated as follows:

$$
M_{f f}=\frac{w_{9}}{w_{8}} \times \frac{w_{8}}{w_{7}} \times \frac{w_{7}}{w_{6}} \times \frac{w_{6}}{w_{5}} \times \frac{w_{5}}{w_{4}} \times \frac{w_{4}}{w_{3}} \times \frac{w_{3}}{w_{2}} \times \frac{w_{2}}{w_{1}} \times \frac{w_{1}}{w_{T .0}}=0.586
$$

Fuel weight can be obtained from:

$$
W_{F}=\left(1-M_{f f}\right) W_{T . O}+K\left(1-M_{f f}\right) W_{T . O}
$$

Assuming that $W_{F_{\text {Reserve }}}$ is a fraction of $F_{\text {Used }}$ then as defined in Roskam this fraction is 0.25 ,now:

$$
W_{F_{\text {Reserve }}}=0.25 F_{\text {Used }}
$$

So the equation has led to:

$$
\begin{gathered}
W_{F_{G u e s s e d}}=1.25\left(1-M_{f f}\right) W_{T . O} \\
W_{F_{\text {Guessed }}}=388125 \mathrm{lbs}
\end{gathered}
$$

## 4.2-Finalizing Take-Off Weight

Now it's time to get what we wanted from the first place!

### 4.2.1-Calculating Operating Empty Weight (Tent)

$W_{O E_{t e n t}}$ can be obtained from the following formula:

$$
W_{O E_{\text {tent }}}=W_{T . O}-W_{F}-W_{P L}=267875 \mathrm{lbs}
$$

### 4.2.2-Calculating Empty Weight (Tent)

Also for the temporary experimental $W_{\mathrm{E}}$ we can use this formula:

$$
W_{E_{\text {tent }}}=W_{O E_{\text {tent }}}-0.005\left(W_{T . O}\right)-W_{\text {Crew }}
$$

And the crew weight was:

$$
W_{C r}=2050 l b s
$$

And the payload weight:

$$
W_{P L}=94000 \mathrm{lbs}
$$

So in conclusion:

$$
W_{E_{\text {tent }}}=262075 \mathrm{lbs}
$$

### 4.2.3-Allowable Amount of Empty Weight

### 4.2.3.1-Looking for A and B

In this stage to calculate the value of $W_{E}$ we need A and B . To obtain the values of A and B logarithmic graph $W_{T . O}-W_{E}$ for the data base in Excel should be drawn. from The points obtained in this chart, we draw a line that equation gives us A and B values and they should be close to The amounts in the table 1.52 of Roskam book.

A and B values are 0.0833 and 1.0383, respectively for a transport jet aircraft.

### 4.2.3.2- A and B Graph

First, charting $\log W_{T . O}$ vs $\log W_{E}$ for all the planes in the data base, values for A and B Roskam was far from normal values. That's why we have to remove some peer aircrafts data. By deleting some data from peer planes A and B were as follows:


Figure $1 \log \left(W_{T . O}\right)$ vs $\log \left(W_{E}\right)$

$$
\log W_{T . O}=1.0315 \log W_{E}+0.1375
$$

### 4.2.3.3-Finding the Exact Allowable Empty Weight

According to A and B obtained, allowable $W_{E}$ is obtained from the following formula:

$$
W_{E}=i n v \log \left(\log \frac{W_{T . O}-A}{B}\right)=268150.6 \mathrm{lbs}
$$

### 4.2.4-Finalizing Take-Off Weight

Finally, we should obtain error percentage difference between the amount of allowable and tented $W_{E}$.

Optimum take-off weight of aircraft should be close to the target (B777-300ER) and the margin of error is under $0.5 \%$.

But with A and B obtained from peer aircrafts data base, margin of error below $0.5 \%$ is above from the target planes weight which its error percentage difference was too far from target aircraft weight.

But because of $30 \%$ graphs error, numbers for A and B, are not accurate. As a result, we have to manually reach to a minimum error.


| W_to | W_fuel | W_oe-ten | w_e-tent | A |  | B |  | W_e |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 750000 | 388125 | 267875 | 262075 |  | 0.15 | 1.056 | 263912.2 | -1837.24 |
| 755000 | 390712.5 | 270287.5 | 264462.5 | 0.15 | 1.056 | 265578.1 | -1115.56 |  |
| 760000 | 393300 | 272700 | 266850 | 0.15 | 1.056 | 267243.3 | -393.291 |  |
| 761000 | 393817.5 | 273182.5 | 267327.5 | 0.15 | 1.056 | 267576.3 | -248.768 |  |
| 762000 | 394335 | 273665 | 267805 | 0.15 | 1.056 | 267909.2 | -104.221 |  |
| 762100 | 394386.8 | 273713.3 | 267852.8 | 0.15 | 1.056 | 267942.5 | -89.7655 |  |
| 762200 | 394438.5 | 273761.5 | 267900.5 | 0.15 | 1.056 | 267975.8 | -75.3094 |  |
| 762300 | 394490.3 | 273809.8 | 267948.3 | 0.15 | 1.056 | 268009.1 | -60.853 |  |
| 762400 | 394542 | 273858 | 267996 | 0.15 | 1.056 | 268042.4 | -46.3964 |  |
| 762500 | 394593.8 | 273906.3 | 268043.8 | 0.15 | 1.056 | 268075.7 | -31.9396 |  |
| 762600 | 394645.5 | 273954.5 | 268091.5 | 0.15 | 1.056 | 268109 | -17.4825 |  |
| 762700 | 394697.3 | 274002.8 | 268139.3 | 0.15 | 1.056 | 268142.3 | -3.02524 |  |
| 762720 | 394707.6 | 274012.4 | 268148.8 | 0.15 | 1.056 | 268148.9 | -0.13376 |  |
| 762725 | 394710.2 | 274014.8 | 268151.2 | 0.15 | 1.056 | 268150.6 | 0.589115 |  |
| 762750 | 394723.1 | 274026.9 | 268163.1 | 0.15 | 1.056 | 268158.9 | 4.203488 |  |

$$
\mathrm{A}=0.15 \mathrm{~B}=1.056
$$

So in conclusion:

$$
\begin{gathered}
W_{T O}=762725 \mathrm{lbs} \\
W_{E}=\operatorname{inv} \log \left(\log \frac{W_{T . O}-A}{B}\right)=268150.6 \mathrm{lbs} \\
W_{\text {fuel }}=1.25(1-0.586) \times 762725 \\
W_{\text {OE tent }}=762725-W_{\text {fuel }}-\left(W_{P L}=94000\right) \\
W_{E \text { tent }}=W_{\text {OE tent }}-(0.005 \times 762725)-\left(W_{\text {Crew }}=2050\right)
\end{gathered}
$$

| $W_{\text {TO }}$ | $W_{\text {fuel }}$ | $W_{\text {OE tent }}$ | $W_{E \text { tent }}$ | A | B | $W_{E}$ | Diff |
| :---: | :---: | :---: | :--- | :---: | :---: | :---: | :---: |
| 762725 | 394710.2 | 274014.8 | 268151.2 | 0.15 | 1.056 | 268150.6 | 0.589115 |

4.2.6-Table of Calculations

Take Off Weight

| $W_{\text {T. }}$ Guess | 680000 lbs |  |
| :---: | :---: | :---: |
| V | $V_{C r}=482.27$ |  |
|  | $V_{T . O}=186.83$ |  |
|  | $V_{C l}=334.55$ |  |
|  | $V_{F l y}=250$ |  |
| $R$ | $R_{C l}=111.51$ |  |
|  | $R_{C r}=6388.49$ |  |
|  | $R_{\text {Fly }}=300$ |  |
| $C_{j}$ | $C_{j}{ }_{C r}=0.46$ |  |
|  | $C_{j_{\text {Loiter }}}=0.6$ |  |
|  | $C_{j_{F l y}}=0.9$ |  |
| $\frac{L}{D}$ | $\left.\frac{L}{D}\right)_{C r}=17.08$ |  |
|  | $\begin{aligned} & \left.\frac{L}{D}\right)_{\text {Loiter }}=19.73 \\ & \left.\frac{L}{D}\right)_{F l y}=11.835 \end{aligned}$ |  |
| Weight Ratio | $\left.\frac{W_{5}}{W_{4}}\right)_{C r}=0.7$ |  |
|  | $\left.\frac{W_{6}}{W_{5}}\right)_{\text {Loiter }}=0.977$ |  |


|  | $\left.\frac{W_{8}}{W_{7}}\right)_{F l y}=0.913$ |  |
| :---: | :---: | :---: |
| $M_{f f}$ | 0.586 |  |
|  | $W_{F_{\text {used }}}=374710.2$ |  |
| W | $W_{P l}=94000$ |  |
|  | $W_{C r}=2050$ |  |
|  | $W_{O E_{\text {tent }}}=274014.8$ |  |
|  | $W_{e_{\text {tent }}}=268151.2$ |  |
|  | $A=0.1375$ |  |
|  | $B=1.0315$ |  |
|  | $A=0.15$ |  |
|  | $B=1.056$ |  |
| $W_{T . O}$ | 762725 |  |
| ERROR | 0.589115 |  |

## 5-Second Step

Now that we have reached an amount of take-off weight, we should do some research about its sensitivity to other parameters, so we can optimum the sizing's.

## 5.1-Sensetivity Studies

It is quite obvious that sensitivity of $W_{T . O}$ to $W_{P L}$ is really important, because as you know, all of our point for building this airplane is to move some payload and make money out of it! So as you can see having more and more payload is what we want, but we don't want our aircraft to crash either! That's why this sensitivity is very serious.

Let's start:

### 5.1.1-Sensetivity of Take-Off to Payload Weight

Roskam book formula 2.27 for takeoff weight to payload weight is:

$$
\begin{gathered}
\frac{\partial W_{T . O}}{\partial W_{P L}}=\frac{B W_{T . O}}{D-C(1-B) W_{T . O}} \\
B=1.056
\end{gathered}
$$

And:

$$
W_{T O}=762725
$$

Then:

$$
\begin{gathered}
C=1-\left(1-M_{f f}\right)-M_{T F O} \\
D=W_{P L}+W_{C r} \\
M_{f f}=0.586 \\
M_{T F O}=0.005
\end{gathered}
$$

According to the mission we defined for $W_{P L}$ and $W_{C r}$ :

$$
\begin{aligned}
W_{P L} & =94000 \mathrm{lbs} \\
W_{C r} & =2050 \mathrm{lbs}
\end{aligned}
$$

As a result, the amount of C and D become as follow:

$$
\begin{aligned}
& C=0.581 \\
& D=96050
\end{aligned}
$$

Then, sensitivity of take-off weight to payload weight is obtained:

$$
\frac{\partial W_{T . O}}{\partial W_{P L}}=6.663887799
$$

This number shows us that take-off weight is a lot sensitive about payload weight. in fact, for example, if we put 1 pound more of payload on, the take-off weight will rise for 6.6638 pounds, which is a lot.so we should be careful of rising the payload weight.

Let's see what happens for other parameters:

### 5.1.2-Sensetivity of Take-Off to Empty Weight

Using the formula 2.29 from Roskam book, $\frac{\partial W_{T . O}}{\partial W_{E}}$ calculated as follows:

$$
\frac{\partial W_{T . O}}{\partial W_{E}}=\frac{B W_{T . O}}{\ln V \log \left[\frac{\log W_{T . O}-A}{B}\right]}
$$

And for:

$$
\mathrm{A}=0.15 \text { and } \mathrm{B}=1.056
$$

Then we have:

$$
\frac{\partial W_{T . O}}{\partial W_{E}}=3.00367631
$$

So empty weight is not as sensitive as payload weight but it is quite important.
And again for more parameter we have:

### 5.1.3-Sensetivity of Take-Off Weight to Range, Endurance, Velocity, SFC and L/D

The parameters range $(\mathrm{R})$, endurance $(\mathrm{E})$, $\mathrm{SFC}(\mathrm{Cj})$ and $\mathrm{L} / \mathrm{D}$ with Y icon will be displayed.
First, we need to calculate sensitivity coefficient F :
$\mathrm{C}=0.581$ and $\mathrm{D}=96050$

$$
F=\frac{-B W_{T O}^{2}\left(1+M_{R e s}\right) M_{f f}}{C W_{T . O}(1-B)-D}
$$

According to Mff and B and $W_{T O}$ obtained in the previous stage and calculated C and D , we have:

$$
F=3723087.874 \mathrm{lbs}
$$

Due to the changes of values, range (R), speed (V), SFC (Cj) and L/D in every phase it is necessary to evaluate the sensitivity of take-off weight to every one of these parameters in all phases.

### 5.1.4-Sensetivity of Take-Off Weight in Cruise Phase

Using the data obtained in the previous stage which are cruising speed $\mathrm{V}(\mathrm{Cr})$, cruise range $\mathrm{R}(\mathrm{Cr})$, Cj and $\mathrm{L} / \mathrm{D}(\mathrm{Cr})$ :

$$
\begin{gathered}
V_{C r}=482.27 \text { knots } \\
R_{C r}=6388.49 \mathrm{~nm} \\
C_{j_{C r}}=0.46 \\
\frac{L}{D}_{C r}=17.08
\end{gathered}
$$

During the cruise phase sensitivity of the above mentioned parameters using formulas in the following table (according to Roskam), is calculated:

Cruise

| $Y=R$ | $\frac{\partial \bar{R}}{\partial Y}=C_{j}\left(V \frac{L}{D}\right)^{-1}=5.584441145 E^{-5}$ | $\frac{\partial W_{T . O}}{\partial Y}=F \times \frac{\partial \bar{R}}{\partial Y}=207.9136511$ |
| :---: | :---: | :---: |
| $Y=C_{j}$ | $\frac{\partial \bar{R}}{\partial Y}=R\left(V \frac{L}{D}\right)^{-1}=0.7755684$ | $\frac{\partial W_{T . O}}{\partial Y}=F \times \frac{\partial \bar{R}}{\partial Y}=2887509.306$ |
| $Y=V$ | $\frac{\partial \bar{R}}{\partial Y}=-R C_{j}\left(V^{2} \frac{L}{D}\right)^{-1}=0.000739546273$ | $\frac{\partial W_{T . O}}{\partial Y}=F \times \frac{\partial \bar{R}}{\partial Y}=-2754.171483$ |
| $Y=\frac{L}{D}$ | $\frac{\partial \bar{R}}{\partial Y}=-R C_{j}\left(V\left(\frac{L}{D}\right)^{2}\right)^{-1}=-0.020887673$ | $\frac{\partial W_{T . O}}{\partial Y}=F \times \frac{\partial \bar{R}}{\partial Y}=-77766.64408$ |

### 5.1.5-Sensetivity of Take-Off Weight in Loiter Phase

Regarding the values of Endurance (E), $C_{j_{L t r}}$ and L/D which have gained before from loiter phase, sensitivity of these parameters in loiter phase for takeoff weight are calculated as follows:

$$
\begin{gathered}
E_{L t r}=0.75 h r \\
C_{j_{L t r}}=0.6 \\
\frac{L}{D_{L t r}}=19.73
\end{gathered}
$$

Loiter

| $Y=E$ | $\frac{\partial \bar{E}}{\partial Y}=C_{j}\left(\frac{L}{D}\right)^{-1}=0.030410542$ | $\frac{\partial W_{T . O}}{\partial Y}=F \times \frac{\partial \bar{E}}{\partial Y}=113221.1214$ |
| :---: | :---: | :---: |
| $Y=C_{j}$ | $\frac{\partial \bar{E}}{\partial Y}=E\left(\frac{L}{D}\right)^{-1}=0.038013177$ | $\frac{\partial W_{T . O}}{\partial Y}=F \times \frac{\partial \bar{E}}{\partial Y}=141526.4017$ |
| $Y=\frac{L}{D}$ | $\frac{\partial \bar{E}}{\partial Y}=-E C_{j}\left(\frac{L}{D}\right)^{-2}=-0.00115601355$ | $\frac{\partial W_{T . O}}{\partial Y}=F \times \frac{\partial \bar{E}}{\partial Y}=-4303.894628$ |

### 5.1.6-Sensetivity of Take-Off Weight in Fly to Alternate Phase

Using the speed and range $V_{F l y} \& R_{F l y}$ defined in the mission and Cj and $\mathrm{L} / \mathrm{D}$ obtained, sensitivity of this phase are:

$$
\begin{gathered}
V_{F l y}=250 \text { knots } \\
R_{F l y}=300 \mathrm{~nm} \\
C_{j_{F l y}}=0.9 \\
\frac{L}{D_{F l y}}=11.835
\end{gathered}
$$

Fly to alternate

| $Y=R$ | $\frac{\partial \bar{R}}{\partial Y}=C_{j}\left(V \frac{L}{D}\right)^{-1}=0.0003041825095$ | $\frac{\partial W_{T . O}}{\partial Y}=F \times \frac{\partial \bar{R}}{\partial Y}=1132.498213$ |
| :---: | :---: | :---: |
| $Y=C_{j}$ | $\frac{\partial \bar{R}}{\partial Y}=R\left(V \frac{L}{D}\right)^{-1}=0.101394169$ | $\frac{\partial W_{T . O}}{\partial Y}=F \times \frac{\partial \bar{R}}{\partial Y}=377499.04042$ |
| $Y=V$ | $\frac{\partial \bar{R}}{\partial Y}=-R C_{j}\left(V^{2} \frac{L}{D}\right)^{-1}=-0.0003650190114$ | $\frac{\partial W_{T . O}}{\partial Y}=F \times \frac{\partial \bar{R}}{\partial Y}=-1358.997855$ |
| $Y=\frac{L}{D}$ | $\frac{\partial \bar{R}}{\partial Y}=-R C_{j}\left(V\left(\frac{L}{D}\right)^{2}\right)^{-1}=-0.00771058326$ | $\frac{\partial W_{T . O}}{\partial Y}=F \times \frac{\partial \bar{R}}{\partial Y}=-28707.17903$ |

Table of Sensitivities:

| Sensitivity |  |
| :---: | :---: |
| Last Step | $W_{T . O}=762725$ |
|  | $W_{P L}=94000$ |
|  | $W_{C r}=2050$ |
|  | $M_{T F O}=0.005$ |
|  | $M_{f f}=0.586$ |
|  | $A=0.15$ |


|  |  |  | $B=1.056$ |
| :---: | :---: | :---: | :---: |
| $W_{T . O}-W_{P L}$ |  |  |  |
| $C=0.581$ |  |  |  |
| $D=96050 \quad \frac{\partial W_{T . O}}{\partial W_{P L}}=6.663887799$ |  |  |  |
| $W_{T . O}-W_{E}$ |  |  |  |
| $\frac{\partial W_{T . O}}{\partial W_{E}}=3.00367631$ |  |  |  |
| $F=3723087.874$ |  |  |  |
| CRUISE |  |  |  |
| $Y=R$ | $\frac{\partial \bar{R}}{\partial Y}=C_{j}\left(V \frac{L}{D}\right)^{-1}=5.584441145 E^{-5}$ |  | $\begin{aligned} \frac{\partial W_{T . O}}{\partial Y}=F \times & \frac{\partial \bar{R}}{\partial Y} \\ & =207.9136511 \end{aligned}$ |
| $Y=C_{j}$ | $\frac{\partial \bar{R}}{\partial Y}=R\left(V \frac{L}{D}\right)^{-1}=0.7755684$ |  | $\begin{aligned} \frac{\partial W_{T . O}}{\partial Y}=F \times & \frac{\partial \bar{R}}{\partial Y} \\ & =2887509.306 \end{aligned}$ |
| $Y=V$ | $\begin{aligned} & \frac{\partial \bar{R}}{\partial Y}=-R C_{j}\left(V^{2} \frac{L}{D}\right)^{-1} \\ &=-0.000739546273 \end{aligned}$ |  | $\begin{aligned} \frac{\partial W_{T . O}}{\partial Y}=F \times & \frac{\partial \bar{R}}{\partial Y} \\ & =-2754.171483 \end{aligned}$ |
| $Y=\frac{L}{D}$ | $\begin{aligned} \frac{\partial \bar{R}}{\partial Y} & =-R C_{j}\left(V\left(\frac{L}{D}\right)^{2}\right)^{-1} \\ & =-0.020887673 \end{aligned}$ |  | $\begin{aligned} \frac{\partial W_{T . O}}{\partial Y}=F \times & \frac{\partial \bar{R}}{\partial Y} \\ & =-77766.64408 \end{aligned}$ |

## LOITER

\(\left.$$
\begin{array}{|c|c|c|}\hline Y=E & \frac{\partial \bar{E}}{\partial Y}=C_{j}\left(\frac{L}{D}\right)^{-1}=0.030410542 & \begin{array}{c}\frac{\partial W_{T . O}}{\partial Y}=F \times \frac{\partial \bar{E}}{\partial Y} \\
=113221.1214\end{array}
$$ <br>
\hline Y=C_{j} \& \frac{\partial \bar{E}}{\partial Y}=E\left(\frac{L}{D}\right)^{-1}=0.038013177 \& \frac{\partial W_{T . O}}{\partial Y}=F \times \frac{\partial \bar{E}}{\partial Y} <br>

=141526.4017\end{array}\right]\)\begin{tabular}{c}
$\frac{\partial W_{T . O}}{\partial Y}=F \times \frac{\partial \bar{E}}{\partial Y}$ <br>
$=Y=\frac{L}{D}$

 

$\frac{\partial \bar{E}}{\partial Y}=-E C_{j}\left(\frac{L}{D}\right)^{-2}=-0.00115601355$
\end{tabular}

Fly to alternate

| $Y=R$ | $\frac{\partial \bar{R}}{\partial Y}=C_{j}\left(V \frac{L}{D}\right)^{-1}=0.0003041825095$ | $\begin{aligned} \frac{\partial W_{T . O}}{\partial Y}=F \times & \frac{\partial \bar{R}}{\partial Y} \\ & =1132.498213 \end{aligned}$ |
| :---: | :---: | :---: |
| $Y=C_{j}$ | $\frac{\partial \bar{R}}{\partial Y}=R\left(V \frac{L}{D}\right)^{-1}=0.101394169$ | $\begin{aligned} & \frac{\partial W_{T . O}}{\partial Y}=F \times \frac{\partial \bar{R}}{\partial Y} \\ &=377499.04042 \end{aligned}$ |
| $Y=V$ | $\begin{aligned} \frac{\partial \bar{R}}{\partial Y}=-R C_{j} & \left(V^{2} \frac{L}{D}\right)^{-1} \\ & =-0.0003650190114 \end{aligned}$ | $\begin{aligned} \frac{\partial W_{T . O}}{\partial Y}=F \times & \frac{\partial \bar{R}}{\partial Y} \\ & =-1358.997855 \end{aligned}$ |
| $Y=\frac{L}{D}$ | $\begin{aligned} \frac{\partial \bar{R}}{\partial Y}=-R C_{j} & \left(V\left(\frac{L}{D}\right)^{2}\right)^{-1} \\ & =-0.00771058326 \end{aligned}$ | $\begin{aligned} \frac{\partial W_{T . O}}{\partial Y}=F \times & \frac{\partial \bar{R}}{\partial Y} \\ & =-28707.17903 \end{aligned}$ |

## 6-Third Step

From now, we are going to look for Matching Diagram (a graph for T/W vs W/S) for all important configurations. This diagram helps a lot; it would show how much thrust do we need in every single configuration.it would show the proper amount of T/W.

For a start, we are now going to research about stall situation of our aircraft, which means the minimum of speed and maximum of $C_{l_{\max }}$.

Now we are going to see what happens to T/W if we got into a stall situation:

## 6.1-Stall Sizing

To obtain $\mathrm{W} / \mathrm{S}$ stall the relation (3.1) we have from Roskam books is:

$$
V_{S}=\left(2(W / S) / \rho C_{l_{\max }}\right)^{1 / 2}
$$

$V_{S}$ is the same as target airplane which is 170 knots.
Because the only stall speed in case we found is Vs(CLEAN) then we have to detect only in clean configuration whom stall speed is 170 knots.
$C_{l_{\max }}$ according to Table 3.1 Roskam book for Take Off and Landing obtained, we have 1.2-1.8 for clean and 1.6-2.2 for take-off and 1.8-2.8 for landing configuration. There is something you should know, our reference book is kind of old, technology is enhancing every single day, so it's a bit better if we raise this type of Roskam's numbers a bit, it's on you how much!

Airport of origin: Kerman airport at an altitude of $1705 \mathrm{~m}(5594 \mathrm{ft})$ above sea level and the air temperature is 100 degrees Fahrenheit.

Now we have to obtain density value in both origin and destination airport which in this case are the same as each other! So:

$$
\begin{gathered}
\rho_{\mathrm{T} . \mathrm{O}} \& \rho_{\mathrm{L}}=\sigma \times \rho_{\mathrm{S} . \mathrm{L}} \\
\sigma=\frac{\delta}{\theta} \\
\delta=\frac{\mathrm{P}_{5594}}{\mathrm{P}_{\mathrm{S} . \mathrm{L}}} \\
\theta=\frac{\mathrm{T}_{5594}}{\mathrm{~T}_{\mathrm{S} . \mathrm{L}}}
\end{gathered}
$$

Get pressure ratio $\delta$ :

$$
\mathrm{P}_{\mathrm{S} . \mathrm{L}}=14.7 \mathrm{Psi}
$$

Interpolation is obtained from standard table for $\mathrm{P}=5594 \mathrm{ft}$

$$
\begin{array}{rr}
\mathrm{P}(\mathrm{psi}) & \mathrm{h}(\mathrm{ft}) \\
12.1 & 5000 \\
11.7 & 6000
\end{array}
$$

Then:

$$
\begin{gathered}
P_{5594}=11.8624 \text { Psi } \\
\delta=0.806965986
\end{gathered}
$$

Temperature ratio $\theta$ :

$$
T_{S . L}=288.16 \mathrm{~K}=518.688 R
$$

And from the mission:

$$
T_{5594 f t}=100^{\circ} \mathrm{F}=559.67 \mathrm{R}
$$

Then:

$$
\theta=\frac{559.67}{518.688}=1.079010889
$$

Pressure and temperature coefficients are calculated then using them to find ratio of density $\sigma$ :

$$
\sigma=\frac{\delta}{\theta}=0.747875664
$$

Since the chance of getting into stall is much more for take-off and landing situations, we only study these two cases.

### 6.1.1-Clean Take-Off Configuration

Stall sizing calculations are usually evaluated at the airport because planes stall mostly in landing or take-off, in order to do this, we need to find the density of Kerman airport, the airport location. so:

At 5594 ft :

$$
\begin{gathered}
\rho / \rho_{S . L}=0.747875664 \\
\rho_{S . L}=0.002377 \\
\rho=0.001777700453 \text { slug } / \mathrm{ft}^{3}
\end{gathered}
$$

In order to find W/S in clean configuration (flaps up) we obtain:

$$
\begin{gathered}
C_{L_{\max } \text { clean }}=1.2 \text { to } 2.2 \\
\mathrm{~V}_{\mathrm{S}}=170 \text { knots }=286.928 \mathrm{ft} / \mathrm{s} \\
\mathrm{~V}_{\mathrm{S}}=\left(2(\mathrm{~W} / \mathrm{S}) / \rho C_{L_{\max }}\right)^{1 / 2} \\
\left.\frac{W}{S}\right)_{S}=\frac{1}{2} \mathrm{~V}_{S \text { tall }}^{2} \rho C_{L_{M a x}}=73.176974512217 C_{L_{\operatorname{Max}}}
\end{gathered}
$$

### 6.1.2-Clean Landing Configuration

Destination Airport: Kerman Airport at an altitude of $1705 \mathrm{~m}(5594 \mathrm{ft})$ above sea level and air temperature of 100 degrees Fahrenheit. And we already have destination airport density.

W/S has the following formula to be calculated:

$$
\left.\frac{W}{S}\right)_{S}=\frac{1}{2} V_{\text {Stall }}^{2} \rho C_{L_{M a x}}
$$

$$
\begin{array}{rll}
\text { With } C_{L_{\text {Max } T . O}} & =2.2 \quad \frac{\mathrm{~W}}{\mathrm{~S}}=160.9893441 \\
\text { With } & C_{L_{\text {Max }}} & =3
\end{array} \quad \frac{\mathrm{~W}}{\mathrm{~S}}=196.4159148
$$

And having these ratios can be used to draw the graphs we were looking for.



Figure 2 Landing and Take-off Sizing for Stall

## 7-Fourth Step

Stall sizing is over and now it's time for take-off, it wouldn't be wrong if we say that take-off phase and its sizing is a bit more important than the other phases, because everything starts from this phase and all off the flight phases are relevant to take-off, so we suggest you to take all safety factor and judgment you want in this phase. Let's begin:

## 7.1-Take-Off Sizing

To get started, we refer to the equation of distance of take-off bond in Far25:

$$
S_{T O F L}=37.5(\mathrm{~W} / \mathrm{S})_{T O} /_{\sigma C_{l_{\max } O}}(T / W)_{T O}
$$

$S_{T O F L}$ from the mission is:

$$
S_{T O F L}=10500 \mathrm{ft}=1.7280778 \mathrm{~nm}
$$

$C_{l_{T . O}}$ can be calculated from Table 3.1 of the reference book (Roskam) and taking into account the relevant numbers (range from 1.6 to 2.2), and as before taking credit for the advancement of technology and the rise of such factors during this years, we define the values. The range includes three numbers (again for range of 1.6 to 2.2), three distinct extraction ratio will be achieved, and of course with a value for $\sigma$ in stall sizing step, which was 0.747875664 , the following ratio can be achieved:

$$
\begin{gathered}
\sigma=0.747875664 \\
C_{l_{\text {max }}}=2.4 \text { Then }(T / W)_{T O} /(W / S)_{T O}=0.001989762884 \\
C_{l_{T . O}}=2.2 \text { Then }(T / W)_{T O} /(W / S)_{T O}=0.002170650419 \\
C_{l_{T . O}}=1.6 \text { Then }(T / W)_{T O} /(W / S)_{T O}=0.002984644326
\end{gathered}
$$

And as before with having these ratios we can draw the graphs we still want!


Figure 3 Take-off Sizing

## 8-Fifth Step

Now we need all the above parameters for landing phase:

## 8.1-Landing Sizing

According to the $S_{L}$ related to the mission from the list defined, can be $S_{F L}$ amount calculated according to the equations for Far 25.

$$
\begin{gathered}
S_{F L}=\frac{S_{L}}{0.6} \\
S_{F L}=\frac{8000}{0.6}=13333.3 \mathrm{ft}
\end{gathered}
$$

After $S_{F L}$ we also find:

$$
\begin{gathered}
S_{F L}=0.3 V_{A}^{2} \\
V_{A}=\sqrt{\frac{S_{F L}}{0.3}}=\sqrt{\frac{13333.33}{0.3}}=210.8185107 \mathrm{Kts}=355.8215155964358587 \mathrm{ft} / \mathrm{s}
\end{gathered}
$$

$V_{A}$ can be calculated, continue using the following formula, the amount of $V_{S}$ which is the stall speed that may occur during landing, obtains.

$$
\begin{gathered}
V_{A}=1.2 V_{S} \\
V_{S}=\frac{210.8185107}{1.2}=175.6820922 \text { Knots }=296.51792966369765736 \mathrm{ft} / \mathrm{s}
\end{gathered}
$$

And now because we've got the value of $V_{S}$, we use this general formula mentioned below, we'll see.

$$
\begin{gathered}
V_{S}=\left(2(W / S) / \rho C_{l_{\max }}\right)^{1 / 2} \\
W / S=\frac{\rho C_{l \max } V_{S} \wedge}{2}
\end{gathered}
$$

In this matter, the insertion of $\rho$ at the destination airport which was 0.001777700453 , sizing Stall calculated, and also taking into account the range includes four members for $C_{l_{\max }}$ in Roskam book Table 3.1, and as always based on advances in technology and other factors, some changes would be necessary.

We can now obtain 4 values for W/S:

$$
\begin{aligned}
& C_{l_{L}}=1.8 \text { Then }\left(\frac{W}{S}\right)_{L}=140.6671776 \\
& C_{l_{L}}=2.3 \text { Then }\left(\frac{W}{S}\right)_{L}=179.7413937 \\
& C_{l_{L}}=2.8 \text { Then }\left(\frac{W}{S}\right)_{L}=218.8156097 \\
& C_{l_{\max _{L}}}=3.0 \text { Then }\left(\frac{W}{S}\right)_{L}=234.4452961
\end{aligned}
$$



Figure 4 Landing Sizing

## 9-Sixth Step

We've now reached the climb phase, because of the nature of this flight phase, we can't talk generally for all of it in all the times, we need to divide it into six configurations, and talk about them one by one, and also in this step we need aircraft drag polar, because the difference between these situations is in the aircraft drag.

## 9.1-Climb Sizing

First we name the configurations we talked about and then aircraft Drag Polar Equation will be determined for each one of them.

- take off flaps, gear down
- take off flaps, gear up
- take off flaps, gear up, no ground effect
- clean configuration
- approach flaps, gear down
- landing flaps, gear down

Aircraft drag polar equation is obtained through the following relations:

$$
\begin{aligned}
& C_{D}=C_{D_{0}}+k C_{L}^{2} \\
& k=\frac{1}{\pi e A R}
\end{aligned}
$$

To obtain the noise coefficient of drag $\left(C_{D_{0}}\right)$ equation 3.20 of Roskam book will be used:

$$
C_{D_{0}}=f / S
$$

S is the area of the wing which is $4605 \mathrm{ft}^{\wedge} 2$ (target airplane) and f is surface fraction that would be obtained from:

$$
\log _{10} f=a+b \log _{10} S_{w e t}
$$

In the above equation a and b are a function of surface friction coefficient $C_{f}$, the value of $C_{f}$ will be obtained from Figure(B) in Page 120 of the Roskam book, for a turbojet aircraft, it is considered 0.003.

$$
C_{f}=0.003
$$

Using Table 3.4 of the Roskam book, a and b can be obtained for different surface frictions $\left(C_{f}\right)$.

$$
\text { For } C_{f}=0.003, \mathrm{a}=-2.5229 \text { and } \mathrm{b}=1 .
$$

Then we calculate $S_{\text {wet }}$ from the following equation:

$$
\log _{10} S_{w e t}=c+d \log _{10} W_{T o}
$$

d and c from Table 3.5, of the Roskam book are 0.0199 and 0.7531 respectively obtained for a turbojet aircraft and have fixed values. And $\mathrm{W}(\mathrm{TO})=762725 \mathrm{lbs}$ (had been done).

$$
\begin{aligned}
& c=0.0199 \& d=0.7531 \\
& S_{w e t}=28178.07541 f t^{2}
\end{aligned}
$$

By calculating the $S_{\text {wet }}$, f is obtained:

$$
f=84.53008915 f t^{2}
$$

By calculating the f and having the s of the target aircraft, $C_{D_{0}}$ is determined.

$$
\begin{gathered}
s=4605 f t^{2} \\
C_{D_{0}}=\frac{f}{S}=0.018356153
\end{gathered}
$$

When calculating the drag polar term, $\Delta C_{D_{0}}$ is defined, which indicates the effect of flap and gear. So drag polar is the relationship we rewrite as follows:

$$
C_{D}=C_{D_{0}}+\Delta C_{D_{0}}+\frac{C_{L}^{2}}{\pi e A R}
$$

According to Table 3.6, Roskam book value $\Delta C_{D_{0}}$ and e can be obtained:

| Configuration | $\Delta C_{D_{0}}$ | E |
| :---: | :---: | :---: |
| Clean | 0 | 0.85 |
| Take off flaps | $0.010-0.020$ | 0.80 |
| Landing flaps | $0.055-0.075$ | 0.75 |
| Landing gear | $0.015-0.025$ | No effects |

As before due to advances in technology, we determine the value of $\Delta C_{D_{0}}$, For the calculation of $C_{D}$, we must obtain AR to the following formula:

$$
A R=b^{2} / S
$$

$b$ and $s$ according to the data base of the target aircraft (B777-300ER) are respectively 212.5833 ft and $4605 \mathrm{ft}^{\wedge} 2$.

$$
\begin{gathered}
\mathrm{S}=4605 \mathrm{ft}^{2} \quad \& \quad \mathrm{~b}=212.58333 \mathrm{ft} \\
A R=9.813606827
\end{gathered}
$$

Then k is obtained, we consider e as 0.85 (due to advances of technology), So:

$$
\begin{gathered}
k=\frac{1}{\pi A R e} \\
K=0.038178843
\end{gathered}
$$

The drag polar relation is to be obtained for the configurations we said before. These parameters were as the same in all of the configurations, but the drag polar isn't so it's Time to obtaining Drag Polar Equations for all of them.

First: Take-off Flaps, gear up

$$
\begin{gathered}
C_{D}=C_{D_{0}}+\Delta C_{D_{0_{\text {To Flaps }}}}+K C_{l}^{2} \\
C_{D}=0.030356153+0.038178843 C_{l}^{2}
\end{gathered}
$$

Second: Take-off Flaps, gear down

$$
\begin{gathered}
C_{D}=C_{D_{0}}+\Delta C_{D_{0 \text { To Flaps }}}+\Delta C_{D_{0_{\text {Landing Gear }}}}+K C_{l}^{2} \\
C_{D}=0.046356153+0.038178843 C_{l}^{2}
\end{gathered}
$$

Third: Clean

$$
C_{D}=C_{D_{0}}+K C_{l}^{2}=0.018356153+0.038178843 C_{l}^{2}
$$

## Fourth: Approach flaps, Gear Down

$$
\begin{gathered}
C_{D}=C_{D_{0}}+\frac{\Delta C_{D_{0_{\text {To Flap }}}}+\Delta C_{D_{0_{\text {Landing Flap }}}}}{2}+\Delta C_{D_{0_{\text {Landing Gear }}}}+K C_{l}^{2} \\
C_{D}=0.068856153+0.038178843 C_{l}^{2}
\end{gathered}
$$

## Fifth: Landing Flaps ,Gear Down

$$
\begin{gathered}
C_{D}=C_{D_{0}}+\Delta C_{D_{0_{\text {Landing Flap }}}+\Delta C_{D_{0_{\text {Landing Gear }}}}+K C_{l}^{2}}^{C_{D}=0.091356153+0.038178843 C_{l}^{2}}
\end{gathered}
$$

Now it's time to separately we T/W (remember we were looking for this as ever.).

## First: Take-off Flaps, gear up, ground effect

In this case $\mathrm{T} / \mathrm{W}$ is obtained from the following formula:

$$
\left(\frac{T}{W}\right)_{T . O}=2\left(\frac{1}{L / D}+0.012\right) \text { at } 1.2 V_{S_{T . O}}
$$

To obtain the L/D, we read the $C_{l_{\text {Max }}^{T . O}}$ from Table 3.1 from the book Roskam for Take-off and due to technological advances took placed this years, we make the value a bit higher, for now we make it 2.4 .

$$
C_{l_{\text {Max }_{T . O}}}=2.4
$$

Now the lift coefficient for this flight conditions is:

$$
C_{l_{T O}}=\frac{C_{l_{\text {Max }} . O}}{(1.2)^{2}}=1.6666667
$$

$C_{l_{T O}}$ obtained in relation to the drag polar, and then we obtain $C_{D}$ for this flight condition:

$$
\begin{gathered}
C_{D}=0.030356153+0.038178843 C_{l}^{2} \\
C_{D}=0.136408494
\end{gathered}
$$

Given the coefficients of lift and drag, L/D is calculated:

$$
\frac{C_{l}}{C_{D}}=\frac{L}{D}=12.21820297
$$

Having obtained L/D so T/W can be calculated in this flight condition:

$$
\left(\frac{T}{W}\right)_{T . O}=0.187690206
$$

T/W obtained is appropriate, for the temperature at airport but we need correction for temperature at every flying conditions. Based on Turbojet aircraft data and the example Roskam made for us, the temperature correction is 0.8 . so $\mathrm{T} / \mathrm{W}$ obtained, shall be divided by 0.8 .

$$
\left(\frac{T}{W}\right)_{T . O}=\frac{0.187690206}{0.8}=0.234612757
$$

Second: Take off Flaps, gear down, ground effect
In this step, as the first step works as follows:

$$
\begin{gathered}
\left(\frac{T}{W}\right)_{T . O}=2\left(\frac{1}{L / D}+0\right) \text { at } 1.1 V_{S_{T . O}} \\
C_{l_{L O f}}=\frac{2.4}{(1.1)^{2}}=1.983471074 \\
C_{D}=0.046356153+0.038178843 C_{l}^{2} \\
C_{D}=0.196557734 \\
\frac{C_{l}}{C_{D}}=\frac{L}{D}=10.09103551 \\
\left(\frac{T}{W}\right)_{T . O}=0.198195715
\end{gathered}
$$

And taking into account its previous state, in this case T/W obtained should be divided by 0.8 .

$$
\left(\frac{T}{W}\right)_{T . O}=\frac{0.198195715}{0.8}=0.247744644
$$

Third: Take off Flaps , gear up ,no ground effect
In this step, as are the cases acted before and the only difference in this case is that in this case with the first configuration of the aircraft is that in this case aircraft is not affected by the Ground Effect.

$$
\begin{gathered}
\left(\frac{T}{W}\right)_{T . O}=2\left(\frac{1}{L / D}+0.024\right) \text { at } 1.2 V_{S_{T . O}} \\
C_{l_{L o f}}=\frac{2.4}{(1.2)^{2}}=1.6666667 \\
C_{D}=0.030356153+0.038178843 C_{l}^{2} \\
C_{D}=0.13640894 \\
\frac{C_{l}}{C_{D}}=\frac{L}{D}=12.21816302 \\
\left(\frac{T}{W}\right)_{T . O}=0.211690728
\end{gathered}
$$

And taking into account the first step, T/W divided by 0.8 , we obtain.

$$
\left(\frac{T}{W}\right)_{T . O}=\frac{0.211690728}{0.8}=0.26461341
$$

Forth: Clean

In this case we have to act like the steps before:

$$
\begin{gathered}
\left(\frac{T}{W}\right)_{T . O}=2\left(\frac{1}{L / D}+0.012\right) \text { at } 1.25 V_{S} \\
\text { For } C_{\text {lmax }}=1.9 \text { Then } C_{l}=\frac{1.9}{(1.25)^{2}}=1.216 \\
C_{D}=0.018356153+0.038178843 C_{l}^{2} \text { so } C_{D}=0.074809528 \\
\frac{C_{l}}{C_{D}}=\frac{L}{D}=16.25461398 \\
\left(\frac{T}{W}\right)_{T . O}=0.147041986
\end{gathered}
$$

The T/W we have achieved is maximum continuous thrust. While the amount of acceptable for a turbojet aircraft is the Trust continued to maximum thrust at take-off that is 0.94 . With this correction and temperature correction too, the following is obtained:

$$
\left(\frac{T}{W}\right)_{T . O}=\frac{0.147041986}{0.94 * 0.8}=0.195534557
$$

Fifth: Approach Flaps , gear down
Again we act like before:

$$
\begin{gathered}
\left(\frac{T}{W}\right)_{L}=\left(\frac{1}{L / D}+0.032\right) \text { at } 1.3 V_{S_{L}} \\
C_{l}=\frac{3}{(1.3)^{2}}=1.775147929 \\
C_{D}=0.068856153+0.038178843 C_{l}^{2} \\
C_{D}=0.18916342 \\
\frac{C_{l}}{C_{D}}=\frac{L}{D}=9.384202976 \\
\left(\frac{T}{W}\right)_{L}=0.138562059
\end{gathered}
$$

To obtain $\left(\frac{T}{W}\right)_{T . O}$ in this configuration we should multiply $\left(\frac{T}{W}\right)_{L}$ to $\frac{W_{L}}{W_{T O}}$.
The $W_{T . O}$ was 762725 lbs and also $W_{L}$ amount equals to the amount $W_{L}$ of the target aircraft (B777-300ER) which is 544000 lbs , For temperature correction, the statement must be divided by 0.8 . So $\left(\frac{T}{W}\right)_{T . O}$ is given by:

$$
\left(\frac{T}{W}\right)_{T . O}=\frac{(T / W)_{L} \times{ }^{W_{L}} / W_{T . O}}{0.8}=0.123533646
$$

## Sixth: Landing Flaps, gear down

As the fifth mode worked, follows with:

$$
\begin{gathered}
\left(\frac{T}{W}\right)_{L}=2\left(\frac{1}{L / D}+0.021\right) \text { at } 1.5 V_{S_{L}} \\
C_{l}=\frac{3}{(1.5)^{2}}=1.3333333 \\
C_{D}=0.091356153+0.038178843 C_{l}^{2} \rightarrow C_{D}=0.159229651 \\
\frac{C_{l}}{C_{D}}=\frac{L}{D}=8.373649788 \\
\left(\frac{T}{W}\right)_{L}=0.280844476
\end{gathered}
$$

Just like the fifth stage for weight correction and temperature correction, $\left(T / W_{L}\right)_{L}$ multiplied by the $W_{L} W_{T . O}$ and division on 0.8 .

$$
\left(\frac{T}{W}\right)_{T .0}=\frac{(T / W)_{L} \times{ }^{W_{L}} / W_{T . O}}{0.8}=0.250384141
$$

And finally T/W to W/S in this section:


Figure 5 Climb Sizing

## 10-Seventh Step

Climb sizing is finally over, maneuvering sizing is going to start but keep in mind, it's a very tricky part and also not as much important! Why not important?! Because we are designing a commercial aircraft and it's not for maneuvering! By the way we need to do this anyway! So:

## 10.1-Maneuver Sizing

Vertical balance for Maneuver mode is achieved by Roskam book, relation 3.42.

$$
n w=C_{l} \bar{q} s=1482 \delta M^{2} C_{l} S
$$

According to page 160 Roskam 3.43 relationship $n_{\text {Max }}$ is achieved.

$$
n_{\operatorname{Max}}=\frac{1482 \delta M^{2} C_{l_{\operatorname{Max}}}}{W / S}
$$

From the mission:

$$
\begin{gathered}
M=0.84 \\
C_{l_{\text {Max }}}=2(\text { Table 3.1 P91 }) \\
\delta=\frac{P_{35000 \mathrm{ft}}}{P_{S . L}}=0.235374149 \\
n_{\text {Max }}=\frac{492.2611186}{\mathrm{~W} / \mathrm{S}}
\end{gathered}
$$

And from Roskam 3.45 Equation:

$$
\begin{gathered}
\frac{T}{W}=\frac{\bar{q} C_{D_{0}}}{W / S}+\frac{W / S}{}\left(n_{M a x}\right)^{2} \\
\pi e A R \\
\frac{T}{W}=\frac{4.48720761}{W / S}+\frac{37.8215899}{W / S} \\
\bar{q}=\frac{1}{2} \rho V^{2}=85.8236262201 \text { knots }=244.4859095 \\
\rho_{35000} \text { ft }=0.000738 \\
C_{D_{0}}=0.018356153(\text { Climb Sizing }) \\
V_{C r}=482.27(\text { Weight Estimation }) \\
A R=9.813606827(\text { Climb sizing }) \\
e=0.85
\end{gathered}
$$

So then:

$$
\frac{T}{W}=\frac{42.30941067}{W / S}
$$

Now the graph:


Figure 6 Maneuver Sizing

## 11-Eighth Step

Time to talk about cruise, we like to cruise in this job! Cruise is cheap, easy to reach, easy to design and doesn't tight our hands! So we like it and it's also a major part of time of the flight so its parameters are important. Let's see what happens:

## 11.1-Cruise Speed Sizing

We know Cruise is established as follows:

$$
\begin{aligned}
& T=D=C_{D} \bar{q} S \\
& W=L=C_{l} \bar{q} S \\
& C_{D}=C_{D_{0}}+k C_{L}^{2}
\end{aligned}
$$

Then:

$$
T=C_{D_{0}} \bar{q}+\frac{C_{L}^{2} \bar{q} S}{\pi e A R}
$$

Therefore, by dividing the thrust-to-weight ratio of 3.60 T/W to W/S During the cruise phase of the relationship as follows Roskam obtained.

$$
\begin{aligned}
& \quad \frac{T}{W}=\frac{C_{D_{0}} \bar{q} S}{W}+\frac{W}{\bar{q} S \pi e A R}=\frac{C_{D_{0}} \bar{q}}{W / S}+\frac{W / S}{\bar{q} \pi e A R} \\
& \rho_{35000 f t}=0.000738 \text { Slug } / f_{t}{ }^{3} \\
& C_{D_{0}}=0.018356153(\text { Climb Sizing }) \\
& V_{C r}=482.27=813.98 \mathrm{ft} / \mathrm{s}(\text { Weight Stimation }) \\
& A R=9.813606827(\text { Climb sizing }) \\
& e=0.85 \\
& \bar{q}=244.4859095
\end{aligned}
$$

So the ratio is calculated as follows, T/W to W/S is:

$$
\frac{T}{W}=\frac{W}{S}\left(\frac{4.487820761}{(W / S)^{2}}+0.00015608\right)
$$

And as always we draw the graphs:


Figure 7 Cruise Speed Sizing

## 12-Ninth Step

In this step we talk about direct climb, it's all about how to reach the cruise height and what happens in the middle.

## 12.1-Direct Climb Sizing

Direct Climb splits into two parts, Sizing to ceiling and Time to climb.

### 12.1.1-Sizing to Ceiling

It's about reaching to ceiling height at the very ending of climb. And because of that, rate of climb is its maximum amount. The relation for $R O C)_{\text {Max }}$ is obtained from Roskam 3.4 equation:

$$
R O C)_{M a x}=V\left[\left(\frac{T}{W}\right)-\left(\frac{1}{(L / D)_{M a x}}\right)\right]
$$

For the ROC at its maximum amount, shall be the maximum amount of L/D. L/D have gained maximum of 19.73 as we seen before. $\quad(L / D)_{\text {Max }}=19.73$

The ROC $)_{\text {Max }}$ from Table 3.8 of the Roskam book, we should look for Minimum Required Climb Rate and determine it for the service ceiling.

$$
R O C)_{\operatorname{Max}}=500 \mathrm{ft} / \mathrm{m}=8.333333 \mathrm{ft} / \mathrm{s}
$$

And the speed from above is obtained from the following formula:

$$
\begin{gathered}
V_{C l}=\frac{V_{C r}+V_{T O}}{2} \\
V_{C l}=334.55 \mathrm{Knots}=564.608 \mathrm{ft} / \mathrm{s}
\end{gathered}
$$

Then:

$$
\frac{T}{W}=\frac{(R O C)_{M a x}}{V_{\text {Climb }}}+\frac{1}{(L / D)_{M a x}}=0.0654437399
$$

T/W obtained should be divided by 0.23 to obtain the ratio of thrust to weight in takeoff mode.

$$
\left(\frac{T}{W}\right)_{T .0}=\frac{0.0654437399}{0.23}=0.2845379995652174
$$

Thus, W/S to T/W graph is given in the form:


Figure 8 Sizing to Ceiling

### 12.1.3-Time to Climb

Now we are talking about the full phase of climbing, its process is identical with that one except that the value of ROC is given by the formula of Roskam 3.32.

$$
R O C=R O C_{0}\left(1-\frac{h}{h_{a b s}}\right)
$$

The $R O C_{0}$ amount Rate Of Climb in sea level, h ceiling of the mission are defined and $h_{a b s}$ absolute ceiling.

The $R O C_{0}$ 3.34 Roskam the relationship is given by the formula:

$$
R O C_{0}=\frac{h_{\text {abs }}}{T_{\text {Climb }}} \ln \left(1-\frac{h}{h_{a b s}}\right)^{-1}
$$

From the mission:

$$
\begin{aligned}
& h=35000 \mathrm{ft} \\
& h_{\text {abs }}=40000 \mathrm{ft}(\text { Table } 3.7 \mathrm{P} 151) \\
& T_{\text {Climb }}=20 \mathrm{~min}=1200 \mathrm{Sec}
\end{aligned}
$$

Then:

$$
R O C_{0}=69.31471806 \mathrm{ft} / \mathrm{s}
$$

Therefore, the ROC will be given by:

$$
R O C=8.664339757 \mathrm{ft} / \mathrm{s}
$$

Finally, using the formula 3.34 and values of above, T/W will be obtained.

$$
\begin{gathered}
R O C=\left(\frac{2(W / S)}{\rho\left(C_{D_{0}} \pi e A R\right)^{\frac{1}{2}}}\right)^{\frac{1}{2}}\left[\left(\frac{T}{W}\right)-\left(\frac{1}{L / D}\right)\right] \\
\frac{T}{W}=\frac{R O C+\left(\frac{2(W / S)}{\rho\left(C_{D_{0}} \pi e A R\right)^{\frac{1}{2}}}\right)^{\frac{1}{2}} \frac{1}{L / D}}{\left(\frac{2(W / S)}{\rho\left(C_{D_{0}} \pi e A R\right)^{\frac{1}{2}}}\right)^{\frac{1}{2}}}=\frac{R O C \times\left[\rho\left(C_{D 0} \times A R \times \pi \times e\right)^{1 / 2}\right]^{1 / 2}}{\sqrt{2^{W} / S}}+\frac{1}{(L / D)_{M a x}}
\end{gathered}
$$

And:

$$
\begin{aligned}
& \left.\frac{L}{D}\right)_{\operatorname{Max}}=18.89224421(\text { Cieling Sizing }) \\
& \rho_{5594 \mathrm{ft}}=0.001777700453(\text { Stall Sizing }) \\
& C_{D_{0}}=0.018356153(\text { Climb Sizing }) \\
& A R=9.813606827(\text { Climb Sizing }) \\
& e=0.85
\end{aligned}
$$

Then:

$$
\frac{T}{W}=\frac{0.215126815}{(W / S)^{\frac{1}{2}}}+0.050684237
$$

Finally, by dividing T / W to 0.23 , W/S to T/W graph is given in the form.

$$
\frac{T}{W}=\frac{0.935333979}{(W / S)^{\frac{1}{2}}}+0.220366248
$$

Time to Climb


Figure 9 Time to Climb Sizing
Sizing's are all done, we just put them all in one table:
12.2- Sizing Tables

| Stall Sizing |  |
| :---: | :---: |
| P | $P_{S . L}=14.7 \mathrm{psi}$ |
|  | $P_{5594 f t}=11.8624 p s i$ |
| $T$ | $T_{S . L}=518.688 \mathrm{~K}$ |
|  | $T_{5594 \mathrm{ft}}=559.67 \mathrm{~K}$ |
| $\rho$ | $\rho_{S . L}=0.0023769$ |
|  | $\theta=1.079010889$ |
|  | $\delta=0.806965986$ |
|  | $\sigma=0.747875664$ |
|  | $\rho_{\text {T.O-L }}=0.001777700453$ |
| $C_{L}$ | $C_{L_{T . O}}=2.2$ |
|  | $C_{L_{L}}=3$ |
| $V_{\text {stall }}$ | $V_{\text {Stall }_{\text {clean }}}=286.928 \mathrm{ft} / \mathrm{s}$ |


|  | $\left(\frac{W}{S}\right)_{T . O}=160.9893441$ |
| :---: | :---: |
| $\frac{W}{S}$ | $\left(\frac{W}{S}\right)_{L}=196.4159148$ |

Take Off Sizing

| $C_{l_{\text {T. }}}$ | $C_{l_{T . O_{1}}}=2.4$ |
| :---: | :---: |
|  | $C_{l_{T . O_{2}}}=2.2$ |
|  | $C_{l_{T . O_{3}}}=1.6$ |
|  | $S_{\text {TFOL }}=10500 \mathrm{ft}$ |
|  | $\sigma=0.747875664$ |
| $\frac{T / W}{W / S}$ | $\left(\frac{T}{T} / W{ }^{W} /\right)_{1}=0.001989762884$ |
|  | $\left(\frac{T / W}{W / S}\right)_{2}=0.002170650419$ |
|  | $\left(\frac{T / W}{W / S}\right)_{3}=0.002984644326$ |

Landing Sizing

| $C_{l_{L}}$ | $C_{l_{L_{1}}}=1.8$ |
| :---: | :---: |
|  | $C_{l_{L_{2}}}=2.3$ |
|  | $C_{l_{L_{3}}}=2.8$ |
|  | $C_{l_{L_{4}}}=3$ |
| $\rho_{L}$ | 0.001777700453 |
| $S_{L}$ | 8000 ft |
| $S_{F L}$ | 13333.3 ft |
| $V_{A}$ | $355.8215155964358587 \mathrm{ft} / \mathrm{S}$ |


| $V_{S}$ | $296.51792966369765736^{f t} / S$ |
| :---: | :---: |
| $\frac{W}{S}$ | $\left(\frac{W}{S}\right)_{1}=140.6671776$ |
|  | $\left(\frac{W}{S}\right)_{2}=179.7413937$ |
|  | $\left(\frac{W}{S}\right)_{3}=218.8156097$ |
|  | $\left(\frac{W}{S}\right)_{4}=234.4452961$ |


| Climb Sizing |  |  |  |
| :---: | :---: | :---: | :---: |
| $C_{D_{0}}$ |  |  | $S=4605 f t^{2}$ |
|  |  |  | $b(S p a n)=212.5833 \mathrm{ft}$ |
|  |  |  | $C_{f}=0.003$ |
|  |  |  | $a=-2.5229$ |
|  |  |  | $b=1$ |
|  |  |  | $c=0.0199$ |
|  |  |  | $d=0.7531$ |
|  |  |  | $W_{\text {T. } 0}=762725 \mathrm{lb}$ |
|  |  |  | $S_{w e t}=28178.07541 \mathrm{ft}^{2}$ |
|  |  |  | $F=84.53008915 t^{2}$ |
|  |  |  | $C_{D_{0}}=0.018356153$ |
|  | $\Delta C_{D_{0}}$ | All <br> Configuration $\mathrm{e}=0.85$ | Take Off , Flaps, Gear Up $=0.012$ |
|  |  |  | Take Off , Flaps, Gear Down $=0.028$ |
|  |  |  | Take Off, Flaps, Gear Up, No Ground Effect $=0.012$ |
|  |  |  | Clean $=0$ |
|  |  |  | Approach, Flaps, Gear Down $=0.0505$ |
|  |  |  | Landing, Gear Down $=0.073$ |
|  |  |  | $A R=9.813606827$ |


|  |  | $\mathrm{K}=0.038178843$ |
| :---: | :---: | :---: |
|  |  | $C_{l_{\text {Max }} \text {.O }}=2.4$ |
|  |  | $C_{l_{\text {Max }}^{\text {Clean }}}=1.9$ |
|  |  | $C_{l_{\text {Max }}}=3$ |
|  |  | Take Off , Flaps, Gear Up $=1.6666667$ |
|  |  | Take Off , Flaps, Gear Down $=1.983471074$ |
|  |  | Take Off , Flaps, Gear Up, No Ground Effect $=1.66666667$ |
|  |  | Clean $=1.216$ |
|  | All | Landing , Flaps , Gear Down $=1.775147929$ |
|  | Configuration | Approach, Gear Down $=1.3333333$ |
|  |  | Clean $=1.216$ |
|  |  | Landing , Flaps, Gear Down $=1.775147929$ |
|  |  | Approach, Gear Down $=1.3333333$ |
|  |  | Take Off , Flaps, Gear Up $=0.136408494$ |
|  |  | Take Off, Flaps, Gear Down $=0.196557734$ |
|  | All Configuration | Take Off , Flaps , Gear Up , No Ground Effect $=0.13640894$ |
|  | $\begin{aligned} & C_{D}=C_{D_{0}}+\Delta C_{D_{0}} \\ &+K C_{I}^{2} \end{aligned}$ | Clean $=0.074809528$ |
|  |  | Approach, Flaps, Gear Down $=0.18916342$ |
|  |  | Landing Flaps, Gear Down $=0.159229651$ |
| $\frac{T}{W}$ | $\frac{L}{D}$ | Take Off , Flaps, Gear Up $=12.21820297$ |
|  |  | Take Off, Flaps , Gear Down $=10.09103551$ |
|  |  | $\begin{gathered} \text { Take Off , Flaps , Gear Up, } \\ \text { No Ground Effect }=12.21816302 \end{gathered}$ |
|  |  | Clean $=16.25461398$ |
|  |  | Approach, Gear Down $=9.384202976$ |
|  |  | Landing,Flaps, Gear Down $=8.373649788$ |


| Constant | Landing, Flaps , Gear Down | $\frac{W_{L}}{W_{T . O}}=0.713232161$ |
| :---: | :---: | :---: |
| Constant | Approach, Gear Down | $\frac{W_{L}}{W_{T . O}}=0.713232161$ |
|  | Take Off , Flaps | $U p=0.244781296$ |
|  | Take Off , Flaps, | Down $=0.247744644$ |
| All Configuration | Take Off <br> No Ground | $\begin{aligned} & \text { tps , Gear Up } \\ & c t=0.26461341 \end{aligned}$ |
|  | Clean $=$ | 95534557 |
|  | Approach, Gear | $w n=0.123533646$ |
|  | Landing, Flaps , G | Down $=0.250384141$ |
| Maneuver Sizing |  |  |
|  |  |  |
|  | $\delta_{a t} 35000 \mathrm{ft}$ | 235374149 |
|  |  | 0.84 |
| $T$ | $V_{C r}=$ | $2.27^{f t} / \mathrm{S}$ |
| $\bar{W}$ | $\bar{q}=2$ | 4859095 |
|  | $\rho_{35000 f}$ | 0.000738 |
|  |  | 0.85 |
|  |  |  |



| Direct Climb Sizing |  |
| :---: | :---: |
| Ceiling |  |
| $\frac{T}{W}$ | $C_{D_{0}}=0.018356153$ |
|  | $\frac{L}{D}=19.73$ |
|  | $W_{T . O}=762725 \mathrm{lb}$ |
|  | $R O C=8.333333$ |
|  | $\rho_{a t} 35000 \mathrm{ft}$ $=0.000738$ |
|  | $\frac{T}{W}=0.2845379995652174$ |
|  | $W_{\text {T.O }}=762725 \mathrm{lb}$ |
|  | $\rho_{\text {at } 5594 \mathrm{ft}}=0.001777700453$ |
|  | $H_{C r}=35000 \mathrm{ft}$ |
|  | $H_{a b s}=46000 \mathrm{ft}$ |
|  | ROC) $)_{0}=54.84526807$ |
| $\frac{T}{W}$ | $\frac{T}{W}=\frac{R 0 C\left(\rho\left(C_{D_{0}} \frac{1}{K}\right)^{\frac{1}{2}}\right)^{\frac{1}{2}}}{\sqrt{2\left(\frac{W}{S}\right)}}+\frac{1}{\left.\frac{L}{D}\right)_{\operatorname{Max}}}$ |
|  | $\left.\frac{L}{D}\right)_{\operatorname{Max}}=18.89224421$ |
|  | $A R=9.813606827$ |
|  | $e=0.85$ |
|  | $\rho_{a t 5594 \mathrm{ft}}=0.001777700453$ |
|  | $K=\frac{1}{\pi e A R}$ |
|  | $C_{D_{0}}=0.018356153$ |

## 13-Matching Diagram

It's time to get what we want! Matching Diagram is all we wanted from the first place. With graphing all the sizing's, we have reached till now in one coordinate we can draw matching diagram, so:


In order to find the design area, take a look at this table, the philosophy of this table is that, a part of every sizing chart has best efficiency in designing, it has lower costs and better fulfilling every needs of the mission than the other parts of chart, so we gathered around all of them to choose the best area for design point.

| Sizing Configuration. | Acceptable Zone of The Curve |
| :---: | :---: |
| Stall Speed | Left |
| Take-off Distance | Above |
| Landing Distance | Left |
| Climb | Above |
| Cruise Speed | Above |
| Maneuver | Above |
| Ceiling | Above |
| Time to Climb | Above |

Now we have to locate the design point, a point from the design area which has the maximum of W/S and the minimum of T/W.


## 14-Part II

This section is all about putting the previous data's together, we now have to engineer every part of the aircraft, have in mind that you can use the peer aircrafts data.

## 14.1-Selection of the Overall Configuration

Body conceptual design must be met in the following three aspects:
1- The length
2- Width

## 3- Distance and type of seats

Body length to diameter ratio $\frac{l_{f}}{d_{f}}$ :
The bigger is the $\frac{l_{f}}{d_{f}}$,the body is longer, thus increasing this parameter would make difficulties in take-off Phase for rotation, and with a perfect arc in the bottom of the body we can overcome this problem.

This ratio determines the diameter of the body and determine the number and location of fixed equipment inside the aircraft.

Distances and the number of seats available on aircraft and other fixed equipment's determined by peer aircrafts.

Depending on the arrangement of the seats we determine the width of the body then having
$\frac{l_{f}}{d_{f}}$ we determine the length of the aircraft.

| Airplane type | $l_{f} / d_{f}$ |
| :---: | :---: |
| Boeing777-300ER | 12.8887 |
| Boeing 747-8 | 12.4461 |
| Boeing 777-200LR | 10.8614 |

## 14.2-Dimentional Sketch

The second step in the field of aircraft design, set three overall view planes with foreign size of it, this amounts obtained due to the target aircraft and of course peer aircrafts.


Figure 10 Dimensional Sketch

## 14.3-Design of Cockpit and Fuselage Layouts:

Cabin Cross section two issues to be considered in the design:
1- Getting on and off from airplane for passengers.
2- There are no specific standards on airplane seats.
Finally, we've reached these sizes from target airplane:

## Cabin Width: 19.23 ft

Fuselage Diameter: 20.31 ft


Figure 11 Cabin Cross Section

## 14.4-Selection \& Integration of the Propulsion System:

Usually, aircraft engines are designed according to the ceiling of the flight. Important parameters in this section include:

- Engine Type
- Engine number
- Installation and placement of the engine
- type and number of engines is defined in the mission.
- to determine the location of the engine it is important for the intake of the engine to have the best performance by not breathing any turbulent air.

To select the engine thrust required by the aircraft, we use the matching diagram and the following formula:

$$
T_{a v}=T / W_{W} \times W_{T O}=0.294311351 \times 762725=224478.6252 \mathrm{lbf}
$$

Then for Safety Factor:

$$
S . F=\frac{T_{R e q}}{T_{a v}}
$$

$$
T_{R e q}=1.1 \times 224478.6252=246926.4847 \mathrm{lbf}
$$

This number is divided by the number of engines which stated in the mission (2*Turbofan Engines):

$$
T_{\text {Req }}=123463.2439 \text { lbf For Each Engine }
$$

After a review of our knowledge and view of corporate catalogs engines such as Pratt \& Whitney, Rolls Royce, General Electric, came to the conclusion that GE has the most powerful turbofan engine made, that is GE90-115B model. In the following part, statistics of this engine will be mentioned.

## Dimensions:

| Overall Length | (286,67 inches) |
| :---: | :---: |
| Overall width | (148.38 inches) |
| Overall Height | (154.56 inches) |

Dry Weight: 8761.1 kg (19315 lb.).

## Ratings:

| Rating | GE90-115B |
| :--- | :---: |
| Thrust, kN (lb) | 513,947 |
|  | $(115,540)$ |
|  | 489,304 |
|  | $(110,000)$ |
| Flat rating ambient | 30 |
| temperature, | $(86)$ |
| ${ }^{\circ} \mathrm{C}\left({ }^{\circ} \mathrm{F}\right)$ | 25 |
|  | $(77)$ |

The location of the twin-turbofan engines is under the wing of the aircraft due to Peers and the target aircraft.

## 14.5-Airfoil Selection for Wing \& Tail:

In the design and selection of wings must first define the following parameters for the wings, we have some of these parameters using data to target aircraft:

- Wing Area
- Wing Location
- Wing Section (Airfoil)
- Aspect Ratio (AR)
- Taper Ratio ( $\lambda$ )
- Thickness Ratio ( $t / c$ )
- Sweep Angle ( $\Lambda$ )
- Dihedral Angle $\left(\Gamma_{w}\right)$
- Incidence Angle ( $i_{w}$ )
- Twist Angle ( $\varepsilon_{w}$ )
- Wing Tip
- Fuel Volume

| Wing Area | $4605 f t^{2}$ |
| :---: | :---: |
| Wing Location | Low Wing |
| Wing Section (Airfoil) | Whitcomb-il |
| Aspect Ratio (AR) | 9.813606827 |
| Taper Ratio $(\lambda)$ | 0.29 |
| Thickness Ratio $(t / c)$ | $11 \%$ at $35 \%$ chord |
| Sweep Angle $(\Lambda)$ | $31.64^{\circ}$ |
| Dihedral Angle $\left(\Gamma_{w}\right)$ | $5^{\circ}$ |
| Twist Angle $\left(\varepsilon_{w}\right)$ | $1.5^{\circ}$ |
| Wing Tip | Winglet |
| Fuel Volume | 181283 L |

Root \& Tip Airfoil Selection:
WHITCOMB INTEGRAL SUPERCRITICAL AIRFOIL (Whitcomb-il)



Figure 12 Airfoil Behavior Graph

## Tail Airfoil:

1. NACA 0008il


Cm v Alpha


Figure 13 NACA 0008il Behavior


Cl v Cd


Cm v Alpha


Cl v Alpha


Cd v Alpha


Cl/Cd v Alpha


Figure 14 NACA 0012H Behavior

## 14.7-Empennage Sizing \& Disposition \& For Control Surface Sizing:

One of the most important tasks of the tail is to stable and trim the aircraft, the longitudinal trim is on the Elevator who is installed on the horizontal tail, and transverse-direction trim is on the Rudder who is installed one the vertical tail.

The tail comes in many forms, each designed to be used in certain aircraft. Using the peer aircrafts tail and especially the target aircraft, and the simplicity of the design and weighing less of the conventional tails, we select this type of tail. The area of vertical and horizontal tail, estimated by the peers and the target aircraft.

Then, to estimate the area of control surfaces on the tail, we refer to Tables 8.7 a and 8.7 b in Roskam book and read data $\mathrm{Se} / \mathrm{Sh}$ and $\mathrm{Sr} / \mathrm{S}$ and $\mathrm{Sa} / \mathrm{S}$ for peer aircrafts, then interpolate these values and calculate for your plane.

## 14.8-Class I Method for Landing Gear Sizing \& Disposition:

The only points that are raised in landing gear design are:

- How to connect (installed)
- Retractable landing gear

With respect to these points we choose.
Because of the popularity of the nose gear landings, whom have the same size of wheels that makes airplane to be horizontally on the bond, we use this type of landing gear, and it also makes the aircraft more stable on the ground and enhances pilot's view.


And now a bit closer look to our landing gear:


15-Summerized Table

| MISSION SPECIFICATIONS |  |
| :---: | :---: |
| NUMBER OF PASSENGERS | 400 |
| WEIGHT OF EACH PASSENGER | 175 lbs |
| BAGGAGE OF EACH PASSENGER | 60 lbs |
| PAYLOAD WEIGHT | 94000 lbs |
| NUMBER OF CREWS | 10 lbs |
| WEIGHT OF EACH CREW | 175 lbs |
| BAGGAGE OF EACH CREW | 30 lbs |
| CREW WEIGHT | 2050 lbs |
| CRUISE RANGE | 6500 nm |
| LOITER TIME | 0.75 hours |
| fly to alternate range | 300 nm |
| CRUISE ALTITUDE | 35000 ft |
| CLIMB TIME | 20 min |
| CRUISE SPEED | 0.84 M |
| CRUISE SPEED | 813.9097 fps |
| CRUISE SPEED | 482.27 Knots |
| T.O FIELD LENGTH | 10500 ft |
| T. O FIELD ALTITUDE | 5594 ft |
| T. O FIELD TEMPERATURE | 310.9278 Kelvin |
| LANDING FIELD LENGTH | 8000 ft |
| LANDING FIELD ALTITUDE | 5594 ft |
| LANDING FIELD TEMPERATURE | 310.9278 Kelvin |
| POWER PLANTS TYPE | Turbofan Engine |
| NUMBER OF ENGINES | 2 |
| PRESSURIZATION | 6000 ft . |
| CERTIFICATION | FAR 25 |
| MISSION FUEL FRACTION ESTIMATION |  |
| Cj)CRUISE | 0.46 |
| Cj)LOITER | 0.6 |
| Cj)ALTERNATE | 0.9 |
| (L/D)CRUISE | 17.08 |
| (L/D)LOITER | 19.73 |


| (L/D)ALTERNATE | 11.835 |
| :---: | :---: |
| A | 0.15 |
| B | 1.056 |
| W T. 0 | 762725 |
| MISSION FUEL FRACTION ESTIMATION 2 |  |
| StART WEIGHT FRACTION | 0.99 |
| TAXI WEIGHT FRACTION | 0.99 |
| T. O WEIGHT FRACTION | 0.995 |
| CLIMB WEIGHT FRACTION | 0.98 |
| CRUISE WEIGHT FRACTION | 0.7 |
| LOITER WEIGHT FRACTION | 0.997 |
| DESCENT WEIGHT FRACTION | 0.99 |
| ALTERNATE WEIGHT FRACTION | 0.913 |
| LANDING WEIGHT FRACTION | 0.992 |
| Mff | 0.586 |
| W F | 394710.2 lbs |
| W T. 0 | 762725 lbs |
| W E | 268150.6 lbs |
| C | 0.581 |
| D | 96050 |
| F | 3723087.874 |
| Wto/Wpl | 6.663887799 |
| Wto/We | 3.00367631 |
| Wto/R)Cruise | 207.9136511 |
| Wto/E)Loiter | 113221.1214 |
| Wto/V)Cruise | -2754.171483 |
| Wto/Cj)Cruise | 2887509.306 |
| Wto/(L/D)]Cruise | -77766.64408 |
| Wto/Cj)Loiter | 141526.4017 |
| Wto/(L/D))Loiter | -4303.894628 |
| Wto/R)Alternate | 1132.498213 |
| Wto/Cj)Alternate | 377499.04042 |
| Wto/V)Alternate | -1358.997855 |
| Wto/(L/D)]Alternate | -28707.17903 |


| LANDING DISTANCE SIZING |  |
| :---: | :---: |
| WI/WT. 0 | 0.713232161 |
| DRAG POLAR ESTIMATION |  |
| A | -2.5229 |
| B | 1.00 |
| C | 0.0199 |
| D | 0.7531 |
| Cf | 0.003 |
| CRUISE SPEED SIZING |  |
| CRUISE ALT DENSITY | 0.000738 slug/ft^3 |
| THRUST AT ALT TO S.LTHRUST RATIO | 0.44086329522875 |
| DIRECT CLIMB SIZING |  |
| RCO | $3290.7169842 \mathrm{ft} / \mathrm{min}$ |
| TIME TO CLIMB SIZING |  |
| h_abs | 46000Ft |
| *GAMMA | Less than 15 degree |
| TARGET AIRPLANE DESIGN POINT |  |
| T/W | 0.29754838 |
| W/S | 168.295 |
| SIMILAR AIRPLANE DESIGN POINT (Boeing 777-300) |  |
| T/W | 0.27878787 |
| w/s | 143.322 |
| DESIGN POINT |  |
| T/W | 0.294311351 |
| w/s | 160 |
| OUTPUT TABLE |  |
| T. 0 THRUST | 224478.6252 |
| Part II |  |
| Overall Configuration | Conventional |
| $\frac{l_{f}}{d_{f}}$ | 12.8887 |
| Legroom | 31 in |
| Cabin Width | 19.23 fts |
| Fuselage Length | 242.33333 |
| Fuselage Diameter | 20.31 fts |

Aircraft Design Project | Aero-Designs
\(\left.\begin{array}{|c|c|}\hline \& First Class:22 sits, 61 in pitch <br>
Seat Pitch \& Business Class:70 sits, 39 in pitch <br>

Economy Class:273 sits,32 in pitch\end{array}\right]\)|  | First Class:20 in |
| :---: | :---: |
| Business Class:17 in |  |
| Economy Class:17.5 in |  |


| Vertical Tail Airfoil |  | NACA0008 |  |
| :---: | :---: | :---: | :---: |
| Horizontal Tail Airfoil |  | NACA0012 |  |
| Vertical Tail control Surface Sizing (Srud/SV) |  | 0.35 |  |
| Horizontal Tail control Surface Sizing (Selevator/Sh) |  | 0.23 |  |
| Landing Gear Type |  | Retractable tricycle with two main gear and single steerable nose gear |  |
| AERODYNAMIC PROPERTIES |  |  |  |
| CONFIGURATION | e | DELTA Cd CONF | Vs knots |
| CLEAN | 0.85 | 0 | 170 |
| T.O | 0.85 | 0.012 | 170 |
| LAND | 0.85 | 0.073 | 175.6820922 |
| APPROACH | 0.85 | 0.0505 | 170 |
| GEARS | 0.85 | 0.015 | 170 |
| CRUISE | 0.85 | 0 | 170 |

- All the calculations and conclusions has gathered in the above tables.
- All the numbers have been engineered and they are also open to new changes if necessary.


## 16-Sources

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[^0]:    ${ }^{i}$ Represented to Prof. Farshad Pazooki

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