## Animal Genetics \& Breeding

## BIOSTATISTICS AND COMPUTER APPLICATION

(UNIT - I)


Lecture Notes an Probalidity STinst equint

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## ABOUT

These lecture notes on "Probability" were prepared and delivered to my undergraduate students studying Animal Genetics \& Breeding course. This course was offered during the academic year 2019-20 in the second professional year of Bachelor of Veterinary Science \& Animal Husbandry degree at College of Veterinary \& Animal Sciences, S.V.P.U.A.T, Meerut, Uttar Pradesh, India. This lecture provides basic terminology and concept on probability. Various basic laws and theorems related to probability were also introduced along with explanatory examples. This lecture paves the foundation and linkage between descriptive and inferential statistics thus making it valuable for students to understand forthcoming lectures. I had tried my level best to simplify the concept in easy to understand language. Further constructive suggestions to improve this lecture note are always welcome from its users on my email and whatsapp.

Digitally signed by Kuldeep Kumar Tyagi Date: 2020.08.20 15:30:15 + 05'30'

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## Probability

### 1.1. Probability statement:

Any statement, in which there is an element of uncertainty about the occurrence of some event, is called a probability statement. For example-

1. India may remain number one milk producer in the world for the next 50 years.
2. There may be drought in Western India next year.

### 1.2. Scale / Limits of Probability

| 0 | 0.5 | 1 |
| :---: | :---: | :---: |
| $0 \%$ Certain | $50 \%$ Certain | $100 \%$ Certain |
| $100 \%$ Uncertain | $50 \%$ Uncertain | $0 \%$ Uncertain |

Probability Scale

### 1.3. Probability of an Event

The relative measure of the degree of certainty with which an event can occur can be termed as the probability of the event.

### 1.4. Definition of Probability

There are three approaches in defining probability

1. The classical or mathematical definition
2. The relative frequency definition or the statistical definition
3. The modern definition or the axiomatic approach to probability

### 1.4.1. Classical or mathematical definition

We need to understand a few basic terminologies before we can define probability in mathematical terms.

### 1.4.1.1. Statistical experiment

An experiment having more than one possible outcome is called a statistical experiment. A statistical experiment is also known as a trial.
1.4.1.2. Event

A possible outcome of a trial is called an event.
1.4.1.3. Exhaustive events

A set of events is said to be exhaustive, if it includes all possible outcomes of a trial.

### 1.4.1.4. Favourable events

Such cases that support the occurrence of an event are said to be cases favourable to that event.
1.4.1.5. Equally likely events

If in a trial, the chance of the occurrence of any possible event is the same, the events are said to be equally likely.
1.4.1.6. Mutually exclusive events

If in a trial, the occurrence of an event rules out the simultaneous occurrence of any other possible event, the events are said to be mutually exclusive.

### 1.4.1.7. Definition

If a trial can result in 'n' mutually exclusive, equally likely and exbaustive outcomes and out of which ' $m$ ' outcomes are favourable to an event $A$, the probability of $A$, denoted by $P(A)$, is then

$$
\mathbf{P}(\mathbf{A})=\frac{m}{n}
$$

Example 1.1. A fair dice is thrown. What is the probability that either 1 or 6 will show up? In this example discuss various terms involved in defining mathematical probability?

## Solution 1.1.

Statistical Experiment: Here statistical experiment (trial) consists of throwing a fair dice and observing the outcomes.
Event: When we throw the dice, possibility of occurrence of various outcomes like $1,2,3, \ldots$ are said to be events.
Exhaustive events: The set $\{1,2,3,4,5,6\}$ consist of exhaustive events and includes all possible outcomes of a trial. It means, $n=6$

Favourable events: The set $\{1,6\}$ consist of favourable events that support the occurrence of an event as per the condition given in trial. It means, $\mathrm{m}=2$.
Equally likely events: Each event in the set $\{1,2,3,4,5,6\}$ has equal chances of occurrence and hence known as equally likely events.
Mutually exclusive events: Each event in the set $\{1,2,3,4,5,6\}$ does not affect the occurrence of another event and hence known as mutually exclusive events.

Hence as per the mathematical definition:

$$
\begin{gathered}
\mathbf{P}(\mathbf{A})=\frac{m}{n} \\
\mathrm{P}(\mathrm{~A})=\frac{2}{6}=\frac{1}{3}
\end{gathered}
$$

### 1.4.2. Relative frequency or statistical definition

The probability of getting a favourable event in a repeated trial tends to stabilize after a particular number of repetitions. Now, the number of times an event occurs is its frequency and when this frequency is divided by the total number of trials, we get the relative frequency of the event.

According to the relative frequency definition, when the number of trials becomes sufficiently large, the relative frequency of an event tends to a limit. This limiting value is the probability of the event under consideration.

| Example 1.2. |
| :--- |
| Suppose, we repeat the experiment of parturition in cows and observe the number |
| of times a female calf is born. We shall find that as we increase the number of |
| observations on parturition from say, 10 to 100 to 1000 to 10000 and so on, the |
| relative frequency of getting a female calf will gradually stabilise at $\frac{1}{2}$. |
| Trial No. Sex of Calf born Cumulative freq of <br> favourable event Probability of <br> favourable event <br> 1 Male 0 $\frac{0}{1}=0$ <br> 2 Female 1 $\frac{1}{2}=0.5$ |$.$|  |
| :---: |


| 50 | Female | 29 | $\frac{29}{50}=0.58$ |
| :---: | :---: | :---: | :---: |
| 100 | Male | 41 | $\frac{41}{100}=0.41$ |
| 5500 | Female | 2710 | $\frac{2710}{5500}=0.49$ |
| 9998 | Male | 5002 | $\frac{5002}{9998}=0.5$ |
| 9999 | Male | 5002 | $\frac{5002}{9999}=0.5$ |
| 10000 | Female | 5003 | $\frac{5003}{10000}=0.5$ |

Mathematically, if n is the total number of trials out of which, an event A occurs m times, the probability of A

$$
\mathrm{P}(\mathrm{~A})=\lim _{n \rightarrow \infty} \frac{m}{n}
$$

### 1.4.3. Modern definition | Axiomatic approach to probability

The axiomatic approach to probability can better be understood after going through following concepts.

### 1.4.3.1. Sample space

It is the set of all possible (or exhaustive) outcomes of a trial. The sample space of a trial can be denoted by $S$ and is given by $S=\left\{e_{1}, e_{2}, \ldots \ldots \ldots . e_{n}\right\}$, where, $e_{1}, e_{2}, \ldots \ldots \ldots e_{n}$ are n elementary events. The sample space can further be of

1. Ordered pairs
2. Finite or infinite depending upon whether it consists of finite or infinite number of elements

### 1.4.3.2. Event

An event is any subset of the sample space.

### 1.4.3.3. Occurence of an Event

An event is said to have occurred whenever the outcome of a trial belongs to the relevant event-subset.

According to the modem definition, the probability of an event $A$, denoted by $\boldsymbol{P}(\boldsymbol{A})$ is a real valued set function that associates a real value $\boldsymbol{P}(\boldsymbol{A})$ corresponding to any subset $A$ of the sample space $S$.

## Restrictions | Axioms of probability theory

1. The probability of an event $A$, in a sample space $S$, is a non-negative real number less than or equal to unity, i.e., $0 \leq \mathrm{P}(\mathrm{A}) \leq 1$.
2. The probability of an event that is certain to occur, is unity. Since $S$ is certain to occur, this implies that $\mathrm{P}(\mathrm{S})=1$.
3. If $A_{1}, A_{2}$ and $A_{3}$, are mutually exclusive events in a sample space S , then
$\mathrm{P}\left(A_{1} \cup A_{2} \cup A_{3}\right)=\mathrm{P}\left(A_{1}\right)+P\left(A_{2}\right)+P\left(A_{3}\right)$
The above relation can be generalised to any number of events.
If a sample space $S=\left\{e_{1}, e_{2}, \ldots . . . . . . e_{n}\right\}$ and elementary events $e_{1}, e_{2}, \ldots \ldots \ldots . . e_{n}$ are mutually exclusive

$$
\mathrm{P}(\mathrm{~S})=\sum_{i=1}^{n} P\left(e_{i}\right)=1
$$

### 1.5. Probability Laws

There are certain notations which are used to understand various probability laws. So let us first understand them-

1. If A and B are two events, then $\mathrm{P}(\mathrm{A} \cup \mathrm{B})$ or $\mathrm{P}(\mathrm{A}+\mathrm{B})$ denotes the probability that either, A occurs or B occurs or both occur simultaneously. It can also be interpreted as the probability of the occurrence of at least one of the two events A and B. The symbol $\cup$ above represents 'union' between two events. ( $\operatorname{Read} \mathrm{A} \cup \mathrm{B}$ as ' A union B ').
2. $\mathrm{P}(\mathrm{A} \cap \mathrm{B})$ or $\mathrm{P}(\mathrm{AB})$ denotes the probability of the simultaneous occurrence of both A and $\mathrm{B} .\left(\operatorname{Read} \mathrm{A} \cap \mathrm{B}\right.$ as ${ }^{\prime} \mathrm{A}$ intersection B ').
3. $\mathrm{P}(\mathrm{A} \mid \mathrm{B})$ denotes the conditional probability of the occurrence of A given that $B$ has already occurred.

### 1.5.1. Multiplication law

This law states that the probability of the simultaneous occurrence of the two events $A$ and $B$ is equal to the product of

1. The probability of $A$ and the conditional probability of $B$ given that $A$ has already occurred
or
2. The probability of $B$ and the conditional probability of $A$ given that $B$ has already occurred.
Using notations:

$$
\begin{aligned}
& \mathrm{P}(\mathrm{~A} \cap \mathrm{~B})=\mathrm{P}(\mathrm{~A}) \cdot \mathrm{P}(\mathrm{~B} \mid \mathrm{A})=\mathrm{P}(\mathrm{~B}) \cdot \mathrm{P}(\mathrm{~A} \mid \mathrm{B}) \\
& \mathrm{P}(\mathrm{~B} \mid \mathrm{A})=\frac{P(A \cap B)}{P(A)} \\
& \mathrm{P}(\mathrm{~A} \mid \mathrm{B})=\frac{P(A \cap B)}{P(B)}
\end{aligned}
$$

i.e.

## Example :

One card is drawn from a pack of 52 cards. The card is not replaced in the pack and another card is drawn. What is the probability that both the cards are spade?

## Solution:

Event 1: One card is drawn, find the probability that it is spade

| Events | A | $\bar{A}$ | Total |
| :--- | :---: | :---: | :---: |
| Possibilities | 13 | 39 | 52 |
| Probability | $\frac{13}{52}=\frac{1}{4}$ | $\frac{39}{52}=\frac{3}{4}$ | $\frac{52}{52}=1$ |

Thus, $\mathrm{P}(\mathrm{A})=\frac{1}{4}$
Event 2: One card is drawn, find the probability that it is spade when the previous one has not been replaced

| Events | $\mathrm{B} \mid \mathrm{A}$ | $\bar{B} \mid A$ | Total |
| :--- | :---: | :---: | :---: |
| Possibilities | 12 | 39 | 51 |
| Probability | $\frac{12}{51}$ | $\frac{39}{51}$ | $\frac{51}{51}=1$ |

Thus, $\mathrm{P}(\mathrm{B} \mid \mathrm{A})=\frac{12}{51}$
Therefore, the probability that both the cards drawn are spade

$$
\begin{gathered}
\mathrm{P}(\mathrm{~A} \cap \mathrm{~B})=\mathrm{P}(\mathrm{~A}) \cdot \mathrm{P}(\mathrm{~B} \mid \mathrm{A}) \\
\mathrm{P}(\mathrm{~A} \cap \mathrm{~B})=\frac{1}{4} \times \frac{12}{51}=\frac{3}{51}
\end{gathered}
$$

If two events are mutually exclusive, $\mathrm{P}(\mathrm{B} \mid \mathrm{A})=\mathrm{P}(\mathrm{B})$ and $\mathrm{P}(\mathrm{A} \mid \mathrm{B})=\mathrm{P}(\mathrm{A})$

Therefore,

$$
\mathrm{P}(\mathrm{~A} \cap \mathrm{~B}) \text { or } \mathrm{P}(\mathrm{AB})=\mathrm{P}(\mathrm{~A}) \cdot \mathrm{P}(\mathrm{~B})
$$

## Example:

One card is drawn from a pack of 52 cards. The card is replaced in the pack and another card is drawn. What is the probability that both the cards are spade?
Solution: Here, now two events are mutually exclusive
Event 1: One card is drawn, find the probability that it is spade

| Events | A | $\bar{A}$ | Total |
| :--- | :---: | :---: | :---: |
| Possibilities | 13 | 39 | 52 |
| Probability | $\frac{13}{52}=\frac{1}{4}$ | $\frac{39}{52}=\frac{3}{4}$ | $\frac{52}{52}=1$ |

Thus, $\mathrm{P}(\mathrm{A})=\frac{1}{4}$
Event 2: One card is drawn, find the probability that it is spade when the previous one has not been replaced

| Events | $\mathrm{B} \mid \mathrm{A}=\mathrm{B}$ | $\bar{B} \mid A=\bar{B}$ | Total |
| :--- | :---: | :---: | :---: |
| Possibilities | 13 | 39 | 52 |
| Probability | $\frac{13}{52}=\frac{1}{4}$ | $\frac{39}{52}=\frac{3}{4}$ | $\frac{52}{52}=1$ |

Thus, $P(B \mid A)=P(B)=\frac{12}{51}$
Therefore, the probability that both the cards drawn are spade

$$
\begin{gathered}
\mathrm{P}(\mathrm{~A} \cap \mathrm{~B})=\mathrm{P}(\mathrm{~A}) \cdot \mathrm{P}(\mathrm{~B} \mid \mathrm{A}) \\
\mathrm{P}(\mathrm{~A} \cap \mathrm{~B})=\mathrm{P}(\mathrm{~A}) \cdot \mathrm{P}(\mathrm{~B}) \\
\mathrm{P}(\mathrm{~A} \cap \mathrm{~B})=\frac{1}{4} \times \frac{1}{4}=\frac{1}{16}
\end{gathered}
$$

### 1.5.2. Addition law

This law states that the probability of the occurrence of at least one of the two events (i.e., either A or B or both) is equal to the probability of A plus the probability of B minus the probability of both A and B .
Using notations:

$$
\mathrm{P}(\mathrm{~A} \cup \mathrm{~B})=\mathrm{P}(\mathrm{~A})+\mathrm{P}(\mathrm{~B})-\mathrm{P}(\mathrm{~A} \cap \mathrm{~B})
$$

Using Venn diagram:

$P(A \cup B)=P(A)+P(B) \cdot P(A \cap B)$

## Example:

A dice is thrown. What is the probability of getting a number less than 5 or an odd number?
Solution: The two events are not mutually exclusive, let A be the event of getting a number less than five and $B$ is the event of getting an odd number.
Event : One card is drawn, find the probability that it is spade

| Events | A | B | $\mathrm{B} \mid \mathrm{A}$ |
| :--- | :---: | :---: | :---: |
| Possibilities | 4 | 3 | 2 |
| Probability | $\frac{4}{6}=\frac{2}{3}$ | $\frac{3}{6}=\frac{1}{2}$ | $\frac{2}{4}=\frac{1}{2}$ |

$$
\begin{aligned}
\mathrm{P}(\mathrm{~A} \cup \mathrm{~B}) & =\mathrm{P}(\mathrm{~A})+\mathrm{P}(\mathrm{~B})-\mathrm{P}(\mathrm{~A} \cap \mathrm{~B}) \\
& =\mathrm{P}(\mathrm{~A})+\mathrm{P}(\mathrm{~B})-[\mathrm{P}(\mathrm{~A}) \cdot \mathrm{P}(\mathrm{~B} \mid \mathrm{A})] \quad \text {.... Law of multiplication } \\
& =\frac{2}{3}+\frac{1}{2}-\left[\frac{2}{3} \times \frac{1}{2}\right] \\
& =\frac{7}{6}-\frac{1}{3} \\
& =\frac{7-2}{6} \\
& =\frac{5}{6}
\end{aligned}
$$

1.5.2.1. Mutually exclusive events
$A$ and $B$ are mutually exclusive, that is, the occurrence of $A$ precludes the occurrence of $B$ and vice versa; then, the two events cannot occur simultaneously and $P(A \cap B)=$ 0 . Thus, for two mutually exclusive events $A$ and $B$, the probability of the occurrence of either $A$ or $B$ is equal to the probability of $A$ plus the probability of $B$.

Using notations:

$$
\mathrm{P}(\mathrm{~A} \cup \mathrm{~B})=\mathrm{P}(\mathrm{~A})+\mathrm{P}(\mathrm{~B})
$$

Using Venn diagram:

$P(A \cup B)=P(A)+P(B)$

## Example:

In a game of cards, where a pack contains 52 cards, 4 categories exist namely spade, club, diamond, and heart. If you are asked to draw a card from this pack, what is the probability that the card drawn belongs to either spade or club category.
Solution: The two events are mutually exclusive, let A be the event of getting a spade and $B$ is the event of getting a club.

| Events | A | B |
| :--- | :---: | :---: |
| Possibilities | 4 | 4 |
| Probability | $\frac{4}{52}=\frac{1}{13}$ | $\frac{4}{52}=\frac{1}{13}$ |

$$
\begin{aligned}
\mathrm{P}(\mathrm{~A} \cup \mathrm{~B}) & =\mathrm{P}(\mathrm{~A})+\mathrm{P}(\mathrm{~B}) \\
& =\frac{1}{13}+\frac{1}{13} \\
& =\frac{2}{13}
\end{aligned}
$$

### 1.5.2.2. Exhaustive events

Again, if A and B are the only possible outcomes of a trial (i.e., A and B are exhaustive events), then the occurrence of either $A$ or $B$ is a certainty. We know that the probability of an event that is certain to occur is 1 .
Using notations:

$$
\mathrm{P}(\mathrm{~A} \cup \mathrm{~B})=\mathrm{P}(\mathrm{~A})+\mathrm{P}(\mathrm{~B})
$$

Using Venn diagram:

$P(A \cup B)=P(A)+P(B)$

## Example:

Twenty (25) male and 35 female calves are born at a farm. A calf is selected at random, what is the probability that it will either be a male or female?
Solution: The two events are exhaustive events, hence $\mathrm{P}(\mathrm{A} \cup \mathrm{B})=1$
Proof:

| Events | A | B |
| :--- | :---: | :---: |
| Possibilities | 25 | 35 |
| Probability | $\frac{25}{60}=\frac{5}{12}$ | $\frac{35}{60}=\frac{7}{12}$ |

$$
\begin{aligned}
\mathrm{P}(\mathrm{~A} \cup \mathrm{~B}) & =\mathrm{P}(\mathrm{~A})+\mathrm{P}(\mathrm{~B}) \\
& =\frac{5}{12}+\frac{7}{12} \\
& =\frac{12}{12} \\
& =1
\end{aligned}
$$

... $($ Since $\mathrm{P}(\mathrm{A} \cap \mathrm{B})=0)$

### 1.5.2.3. Complementary events

Suppose A is a possible outcome of some trial. It is clear that the trial either results in the occurrence of $A$ or the nonoccurrence of $A$. Thus, $A$ and 'not A' exhaust all the possible outcomes of any trial. So, if $\bar{A}$ (Read as 'A-bar') denotes 'not A', we have,

Using notations:

$$
\mathrm{P}(\mathrm{~A})+\mathrm{P}(\bar{A})=1
$$

i.e. $\mathrm{P}(\bar{A})=1-\mathrm{P}(\mathrm{A})$

Using Venn diagram:

$\mathrm{P}(\mathrm{A})+\mathrm{P}(\bar{A})=1$
Here, $\bar{A}$ is called complement to the event A . Thus, the sum of probabilities of any event and its complement is always equal to 1

### 1.5. Bayes Theorem

Let $A_{1}, A_{2}$, $\qquad$ $A_{n}$, be ' $n$ ' mutually exclusive and exhaustive events and there is event ' $D$ ' which can occur in conjunction with any of them. If D actually happens, then the conditional probability of the occurrence of $A,(i=1,2,3, \ldots \ldots . . n)$ given $D$, is given by

$$
\begin{aligned}
\mathrm{P}\left(A_{i} \mid D\right) & =\frac{P\left(A_{i} \cap D\right)}{P(D)} \\
\text { Where, } \mathrm{P}(\mathrm{D}) & =\sum_{i=n}^{n}\left(A_{i} \cap D\right)
\end{aligned}
$$

## Example :

The share of total calves born at three farms $A_{1}, A_{2}$, and $A_{3}$ are $25 \%, 35 \%$ and $40 \%$ respectively. of total output respectively. If total 100 calves were born during the year out of which $1.25 \%, 1.4 \%$ and $0.8 \%$ of calves born at respective farms were found to be congenitally deformed. A calf is drawn at random from total congenitally deformed calves born during the year. What is the probability that it was from Farm $A_{1}$, (ii) Farm $A_{2}$, and (iii) Farm $A_{3}$ ?
Solution:

| Events | $A_{1}$ | $A_{2}$ | $A_{3}$ | $\mathrm{D} \mid A_{1}$ | $\mathrm{D} \mid A_{2}$ | $\mathrm{D} \mid A_{3}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Possibilities | 25 | 35 | 40 | 1.25 | 1.4 | 0.8 |
| Probability | $\frac{25}{100}=\frac{1}{4}$ | $\frac{35}{100}=\frac{7}{20}$ | $\frac{40}{100}=\frac{2}{5}$ | $\frac{1.25}{25}=\frac{1}{20}$ | $\frac{1.4}{35}=\frac{1}{25}$ | $\frac{0.8}{40}=\frac{1}{50}$ |

Therefore, $\mathrm{P}(\mathrm{D})=\sum_{i=n}\left(A_{i} \cap D\right)$
$\mathrm{P}(\mathrm{D})=\mathrm{P}\left(A_{1}\right) \cdot \mathrm{P}\left(\mathrm{D} \mid A_{1}\right)+\mathrm{P}\left(A_{2}\right) \cdot \mathrm{P}\left(\mathrm{D} \mid A_{2}\right)+\mathrm{P}\left(A_{3}\right) \cdot \mathrm{P}\left(\mathrm{D} \mid A_{3}\right)$

$$
\begin{aligned}
& =\left[\frac{1}{4} \times \frac{1}{20}\right]+\left[\frac{7}{20} \times \frac{1}{25}\right]+\left[\frac{2}{5} \times \frac{1}{50}\right] \\
& =\frac{1}{80}+\frac{7}{500}+\frac{1}{125} \\
& =\frac{125+140+80}{10000} \\
& =\frac{345}{10000}
\end{aligned}
$$

Now,

$$
\begin{aligned}
& \mathrm{P}\left(A_{i} \mid D\right)=\frac{P\left(A_{i} \cap D\right)}{P(D)} \\
& \mathrm{P}\left(A_{1} \mid D\right)=\frac{P\left(A_{1} \cap D\right)}{P(D)}=\frac{P\left(A_{1}\right) \cdot P\left(D \mid A_{1}\right)}{P(D)} \\
&=\frac{\frac{1}{4} \times \frac{1}{20}}{\frac{345}{10000}} \\
&=\frac{1}{80} \times \frac{10000}{345} \\
&=\frac{10000}{27600} \\
&=\frac{1}{276}
\end{aligned}
$$

Similarly, $\mathrm{P}\left(A_{2} \mid D\right)$ and $\mathrm{P}\left(A_{3} \mid D\right)$ can also be calculated

## ABOUT THE AUTHOR



Dr. Kuldeep Kumar Tyagi had completed his B.V.Sc \& A.H. in the year 2006 from Guru Angad Dev Veterinary and Animal Sciences University, Ludhiana, Punjab India. He got admission in a master program in the subject of Animal Genetics and Breeding at Indian Veterinary Research Institute, Bareilly, Uttar Pradesh, India after securing 6th rank in All India ICAR-JRF examination. He had completed his Masters in the year 2008 and carried out research on competent fibroblast cells used in somatic cell nuclear transfer. He qualified CSIR Net in his first attempt during the final semester of masters program itself. He got selected as Assistant Professor in the year 2009 at College of Veterinary Science \& A.H. at Navsari Agricultural University, Navsari, Gujarat, India. He enriched his practical knowledge and expertise in the subject of Animal Breeding while disbursing his duties as Scheme Incharge at Livestock Research Station of the same university for 9 years. During the same tenure he also accumulated practical expertise on various aspects of field level breeding programs while heading "All India Coordinated Research Project on Goat Improvement - Surti Field Unit" as Principal Investigator. He completed his Ph.D. in the year 2016 from the same university as an inservice candidate. He had worked on gene expression studies on mammary epithelial cells of buffaloes during his Ph.D. degree program. He had handled 5 externally funded and 27 institutionally funded research projects. He had coguided two masters students. He has in his credit 60 research papers, 14 research recommendations and 4 success stories. He is a member of 4 professional societies and attended 21 conferences/ symposiums/ workshops. He has remained on a panel of experts for framing question papers for various Universities and National Testing Agency. He is hosting a google site for online teaching https://sites.google.com/view/learnagb and can be reached at drtyagivet@gmail.com for initiating a conversation.

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